

Shelving spectroscopy of the Sr intercombination line

Adiabatic spin-dependent momentum transfer in a degenerate Sr Fermi gas

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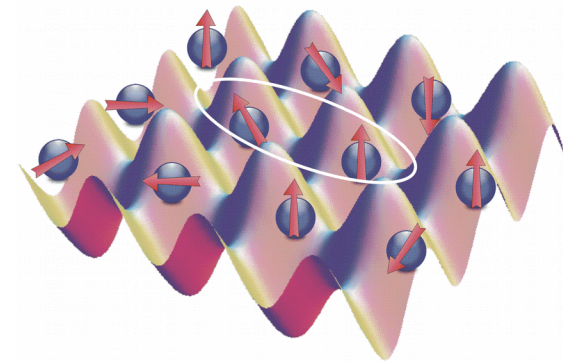
The strontium project at LPL

Implementing quantum magnetism models with ultracold atoms

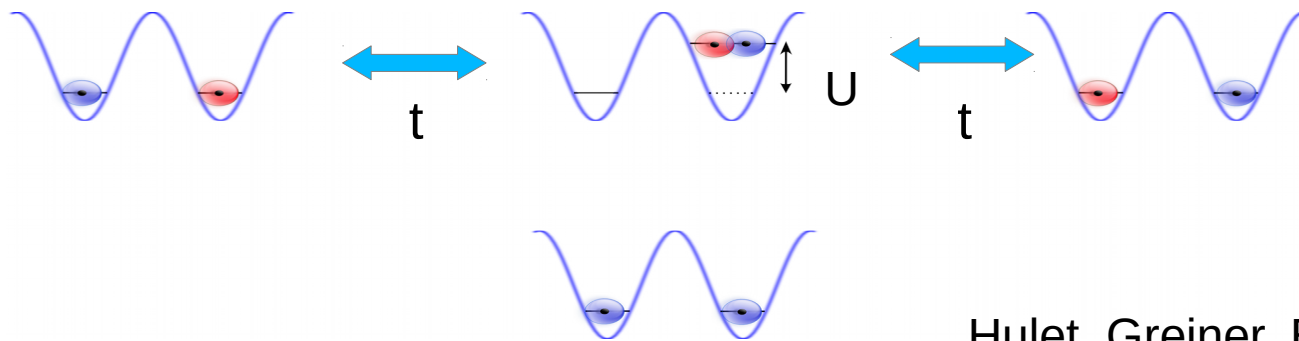
Using ground state atoms, Rydberg state atoms, molecules, ...

Varying the spin-dependence, interaction range, anisotropy...

at LPL : Chromium (long-range anisotropic interactions)
and Strontium (short-range isotropic interactions)



Relevant to both : antiferromagnetic Heisenberg model from super-exchange in the Mott regime



$$H = - J \sum_{\langle i, j \rangle} \vec{S}_i \cdot \vec{S}_j$$

with $J \approx -4t^2/U$

Hulet, Greiner, Bloch, Zwierlein, Kohl, Esslinger, ...

Heisenberg model of magnetism (**effective spin model**)
Tentative model for strongly correlated materials, and
emergent phenomena such as high-Tc superconductivity

Fermionic Strontium 87 in optical lattices: Quantum magnetism beyond spin 1/2 (electron) particles

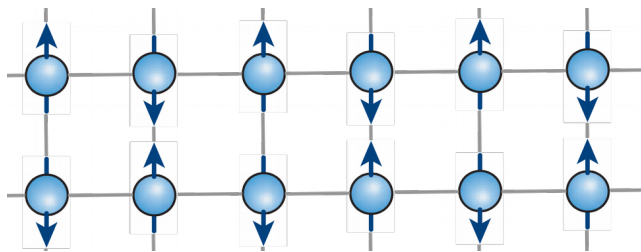
Spin 9/2; SU(10) symmetry

Exploring magnetism with tunable spin degree of freedom

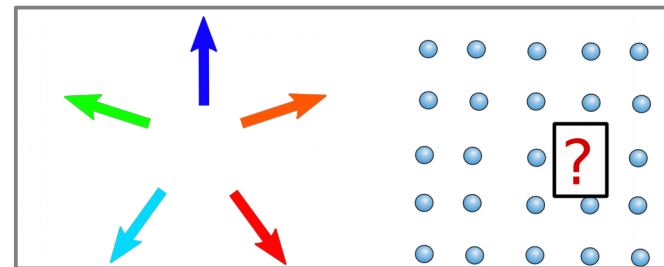
2 spin states: analogy to spin 1/2 electrons

3 spin states: analogy to quarks with three colours

Up to 10 spin states: **no equivalent**



2 states: Neel order



> 5 states : underconstrained magnetism (frustration)

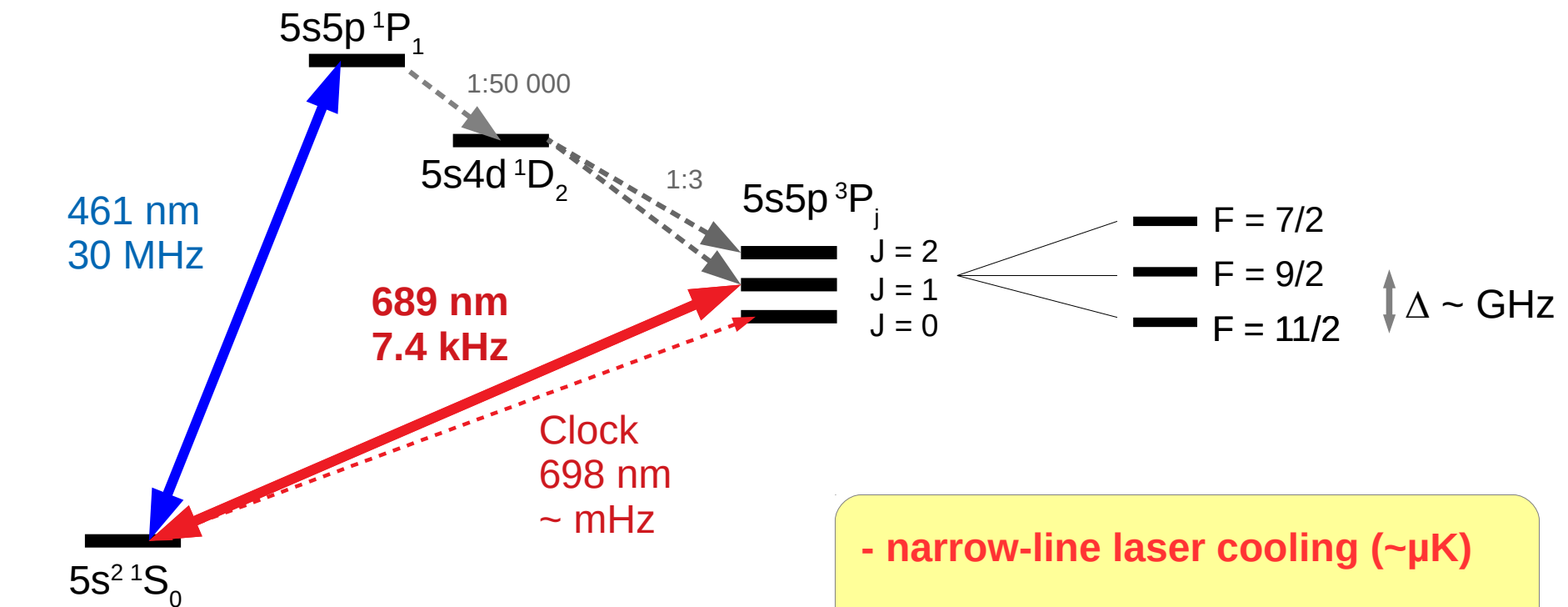
Hermele 2009, PRL **103**, 135301

**Narrow atomic transitions:
new control / probe tools**

Involving a metrology expertise (clock community)

The strontium project at LPL

Two valence electrons
→ singlet and triplet electronic spin states



$^{87}\text{Sr} : I = 9/2$

- narrow-line laser cooling ($\sim \mu\text{K}$)

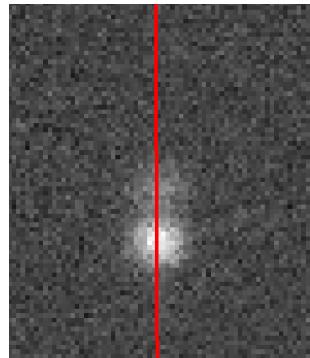
- hyperfine structure: $\Delta \gg \gamma$
Strong spin-dependent conservative forces

Effective magnetic fields;
site-selective spin control

- 1) Shelving spectroscopy of the strontium intercombination line demonstrated on an atomic beam and a hot cell setups
→ applicable to most Sr experiments

[ArXiv:1910.11718](https://arxiv.org/abs/1910.11718)

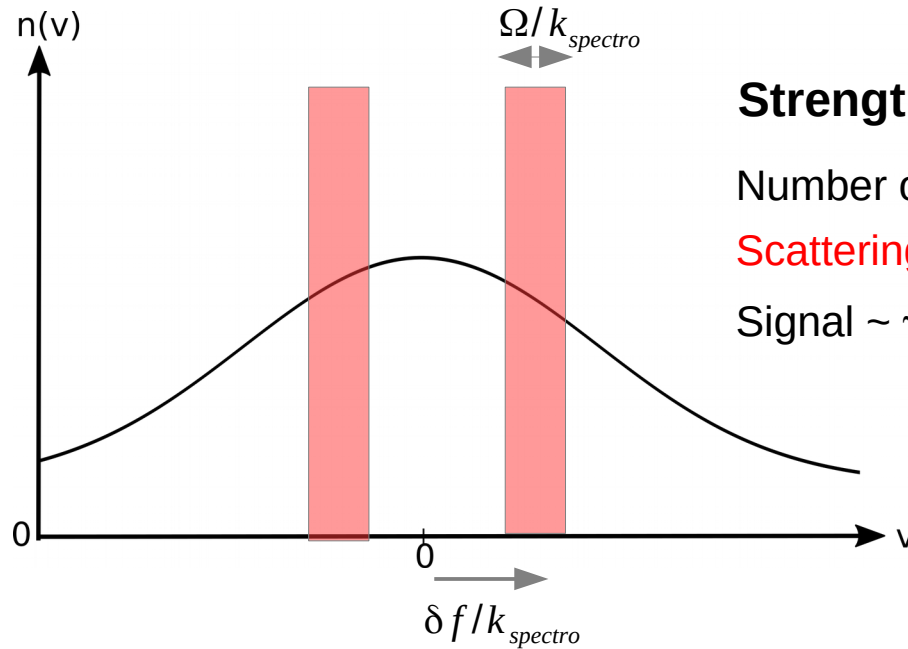
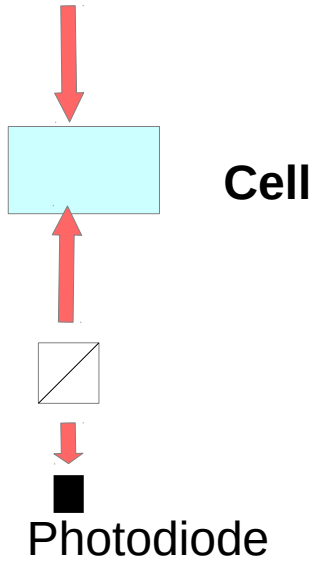
- 2) Birth of the Strontium experiment
 - a degenerate Fermi gas with 10 spin-states
 - first experiments of coherent spin manipulation



Spin-dependent adiabatic momentum transfer

Shelving spectroscopy of the intercombination line

Saturated absorption spectroscopy of a narrow line

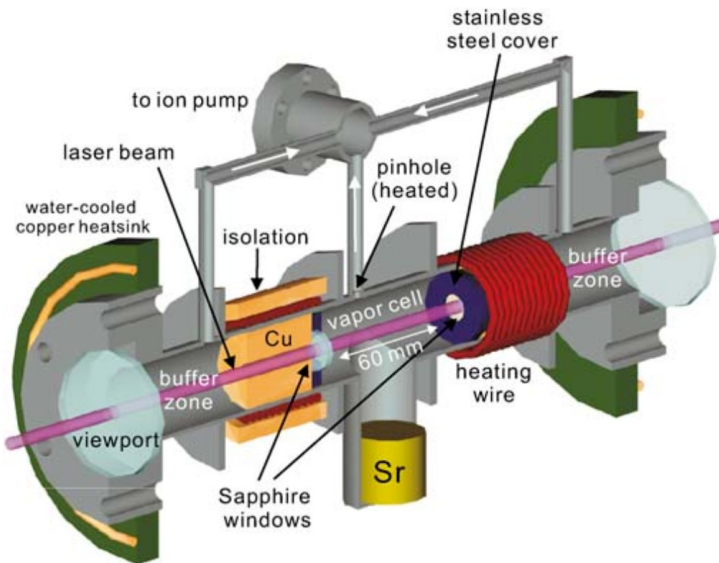


Strength of the signal?

Number of atoms $\sim \gamma$ or Ω

Scattering rate $\sim \gamma$

Signal $\sim \gamma^2$



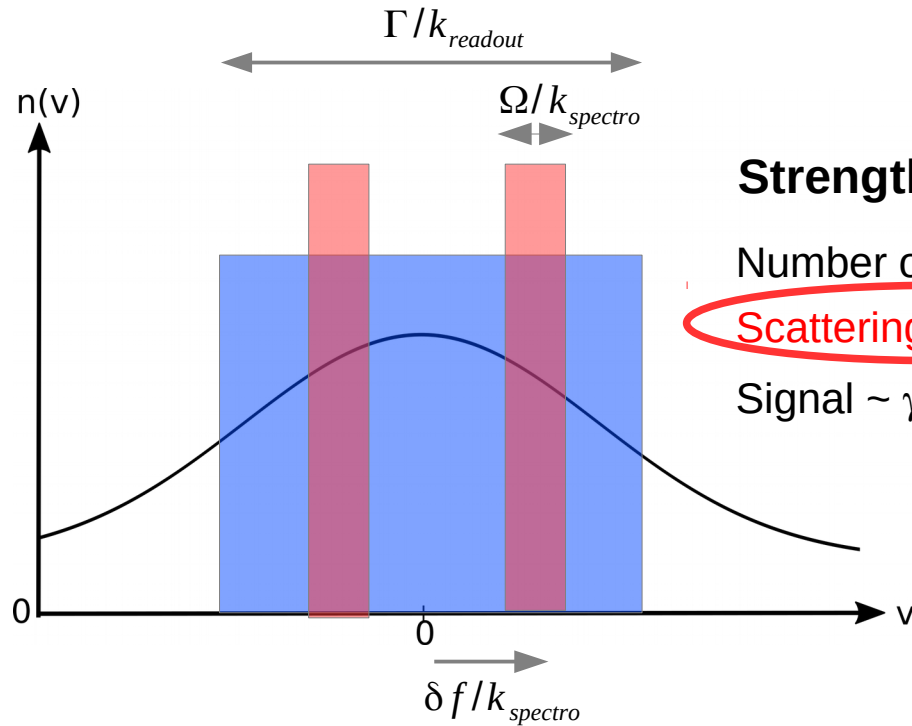
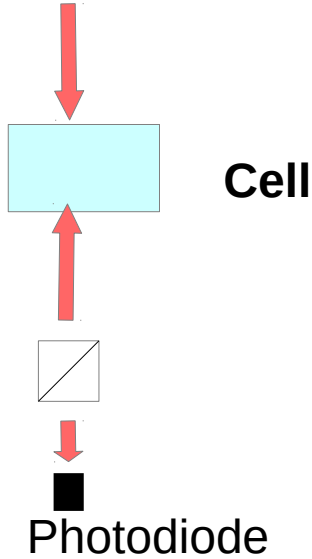
Saturated spectroscopy on the 7kHz wide Sr line

Li 2004, Applied Physics B 78, 315-320: Hot cell

Ferrari 2003, Phys. Rev. Lett. 91, 243002: Atomic beam 10^{-11} relative frequency instability after integration

Shelving spectroscopy of the intercombination line

Saturated absorption spectroscopy of a narrow line



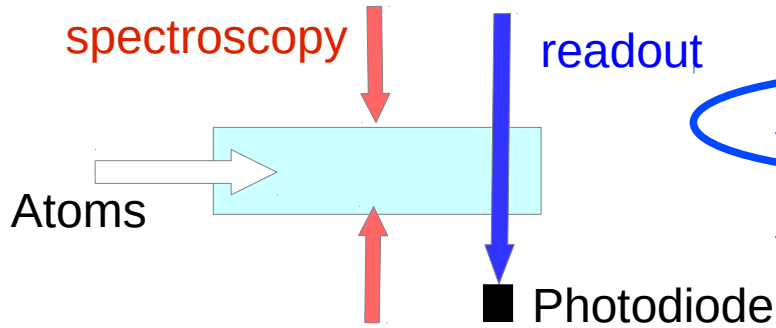
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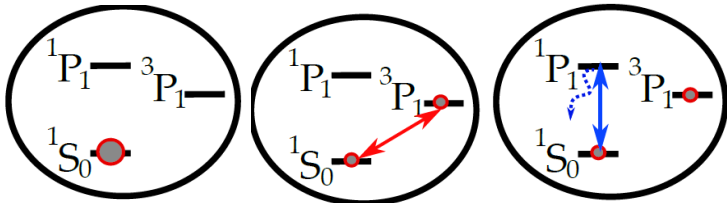
Signal $\sim \gamma^2$

Shelving detection



Scattering rate $\sim \Gamma$

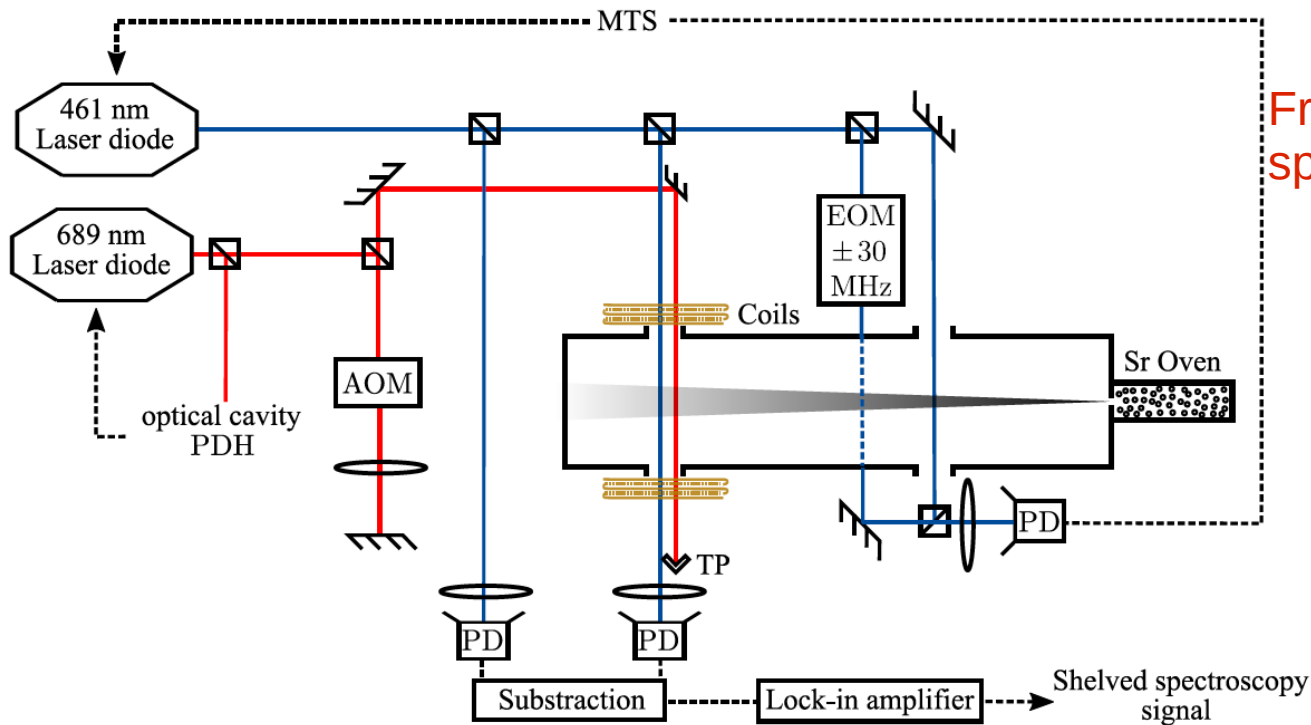
Strontium: $\Gamma/\gamma = 4000$



E.g. thermal Calcium beam clocks:
 Kai-Kai 2006, Chinese Phys Lett 23, 3198
 Mac Ferran 2009, Appl Phys Lett 95, 031103

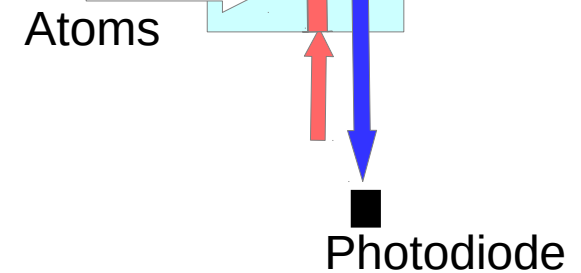
Two independent setups

1) Directed thermal beam



Frequency-modulated spectroscopy

fixed-frequency readout



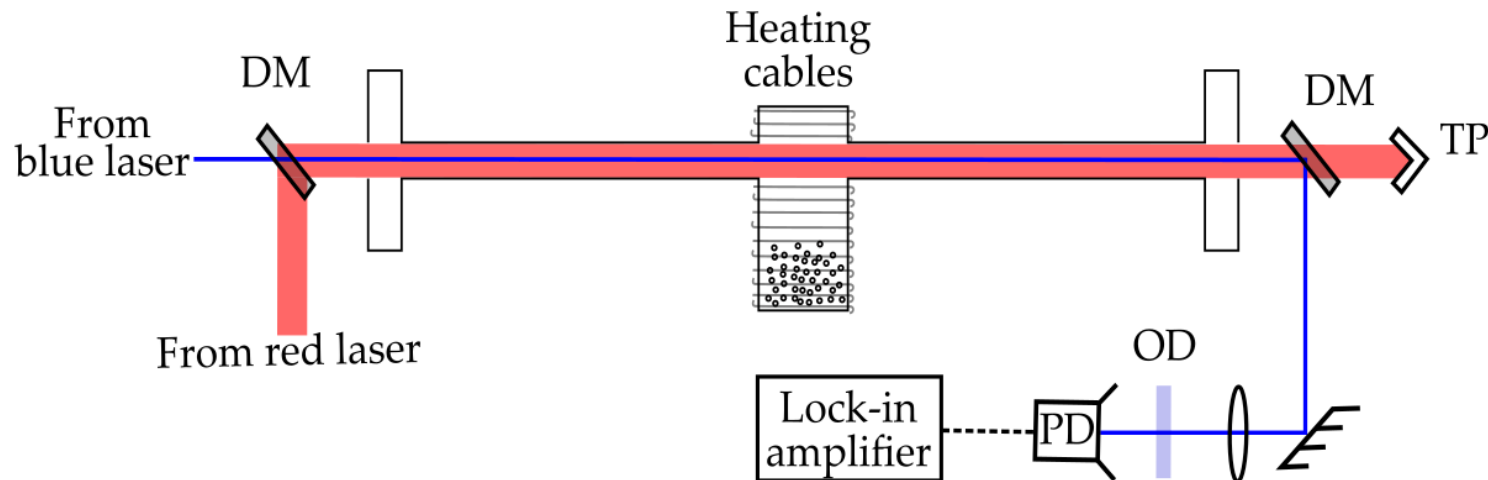
Well defined atomic beam direction

Separated interrogation and readout: compatible with Ramsey schemes

Two independent setups

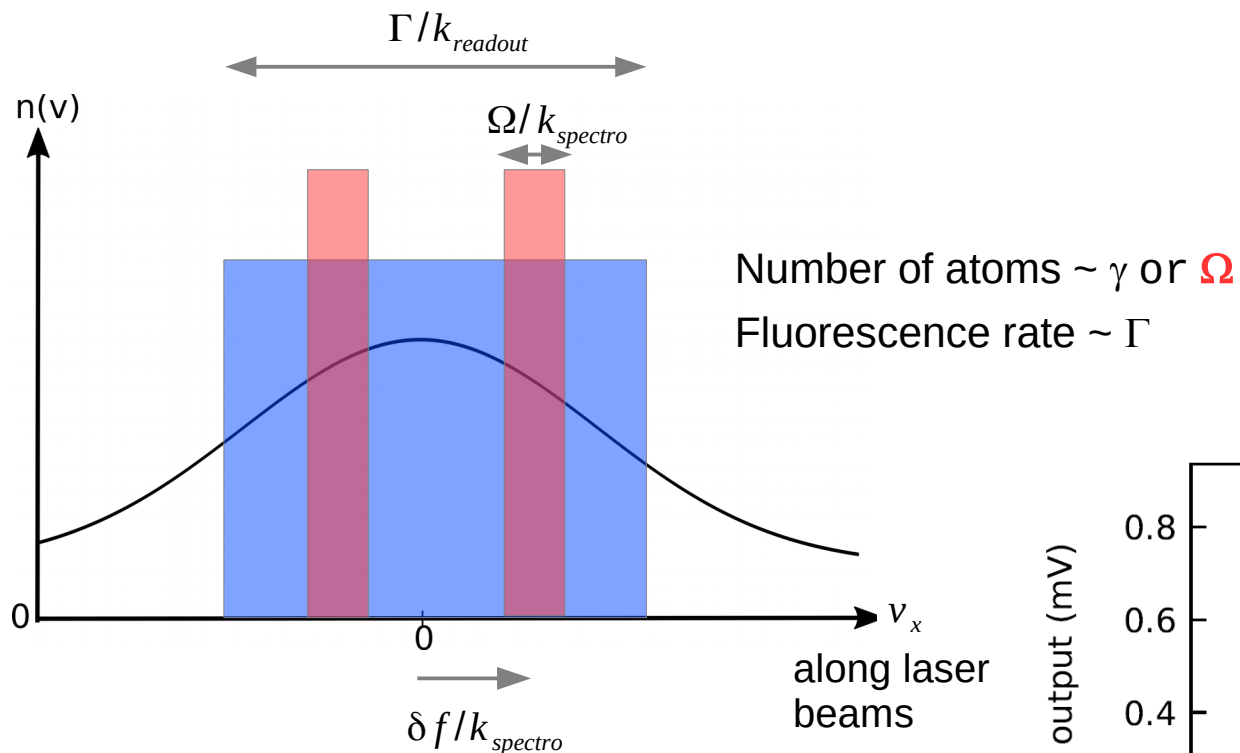
2) Hot vapour cell

Completely independent setup: lasers, detection electronics...



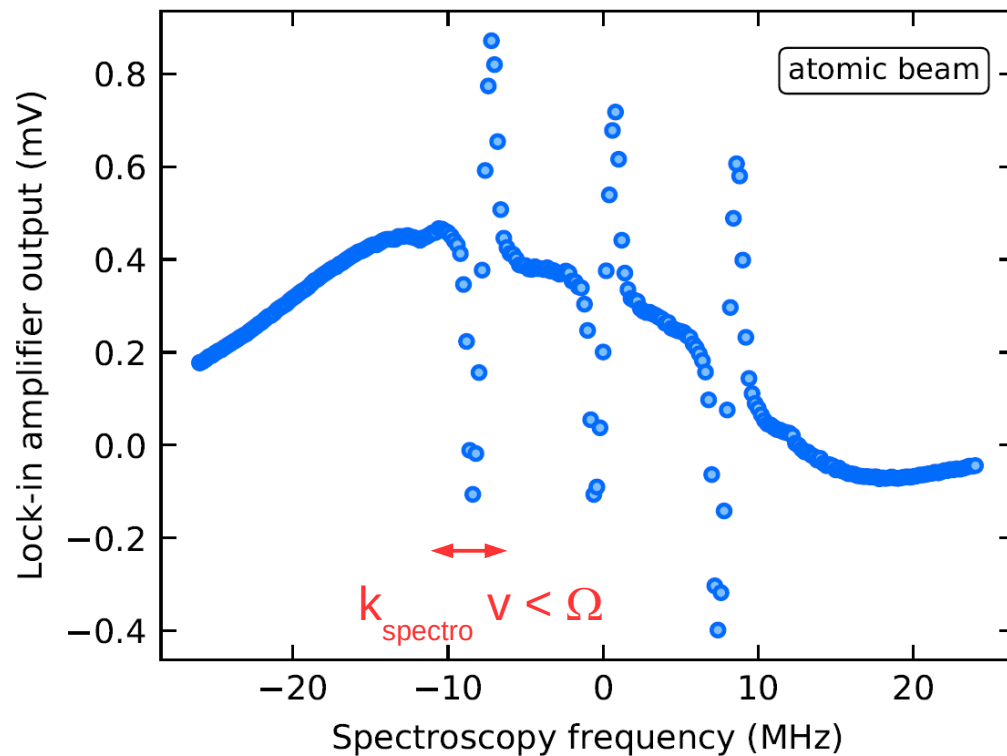
Isotropic velocity distribution
Locally overlapped interrogation and readout

Doppler spectrum overview



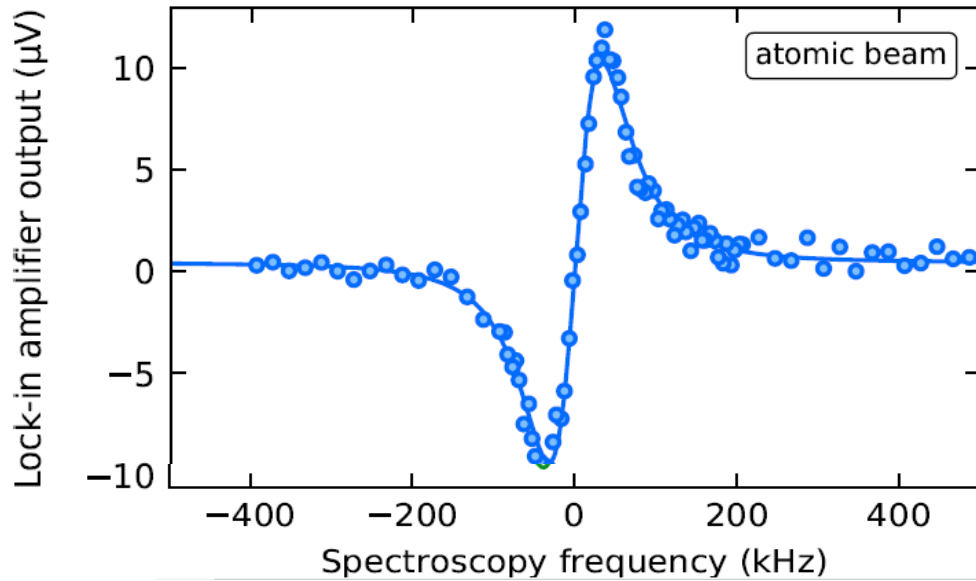
Optimal modulation amplitude (next slide):
the Doppler spectrum becomes negligible

Doppler spectroscopy
of atoms with $k_{\text{readout}} v < \Gamma$



Three lines: $\sigma+$, $\sigma-$, and cross-over (π)
 $g \mu B / h = 7 \text{ MHz}$

SubDoppler line – atomic beam



Lorentzian FWHM : 110 kHz

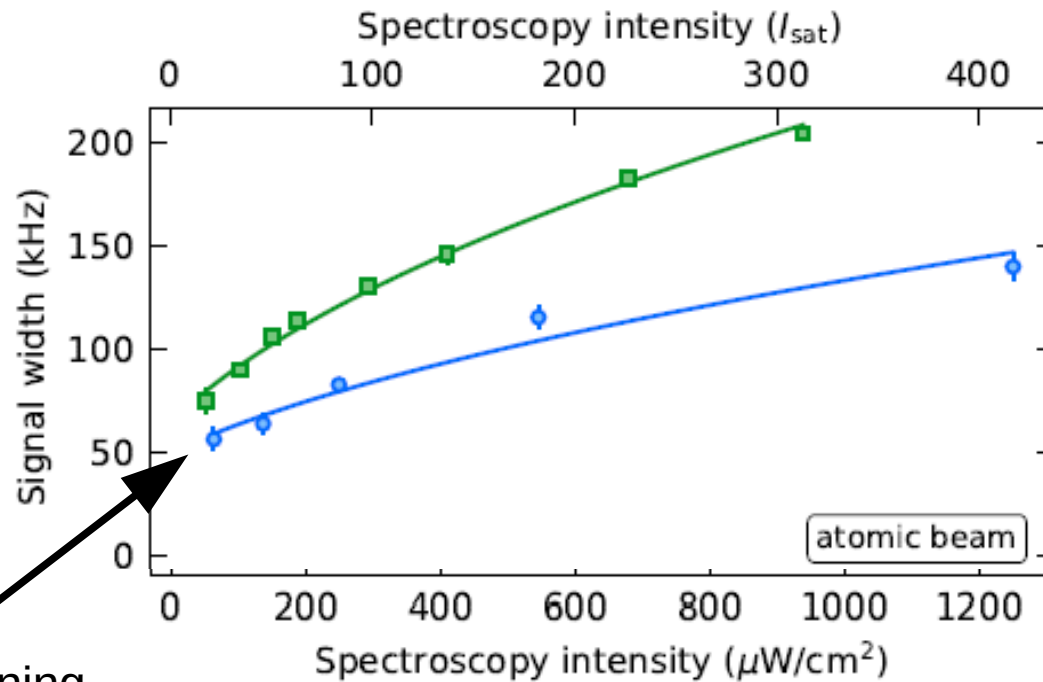
Contributions:

$I = 83 I_{\text{sat}} \rightarrow \Omega = 50 \text{ kHz}$

power broadening FWHM $\sim 70 \text{ kHz}$

Modulation amplitude (p-p) 66 kHz

Transit broadening, FWHM : $\sim 50 \text{ kHz}$

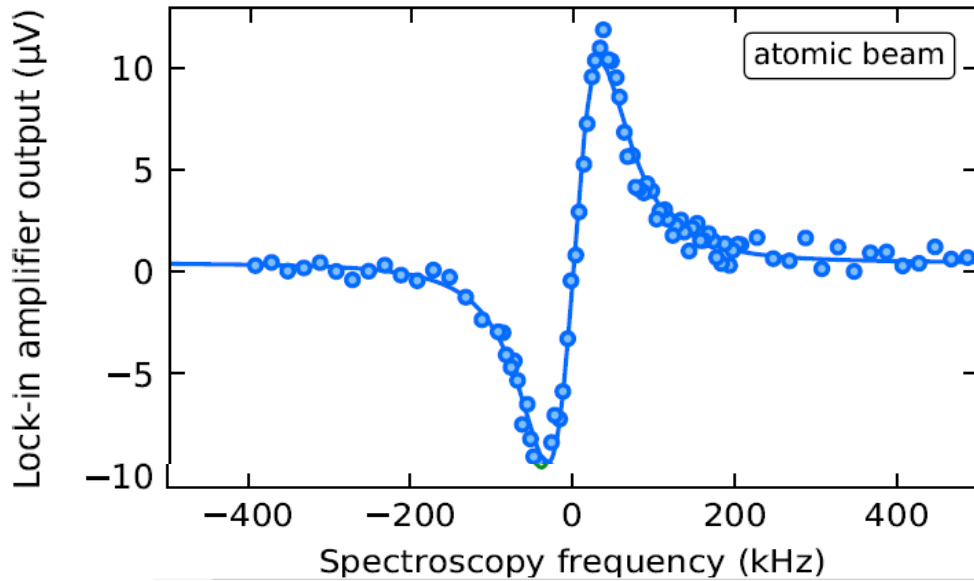


Optimal modulation amplitude scaled

Fixed modulation amplitude 25 kHz p-p

Transit broadening

SubDoppler line – atomic beam



Lorentzian FWHM : 110 kHz

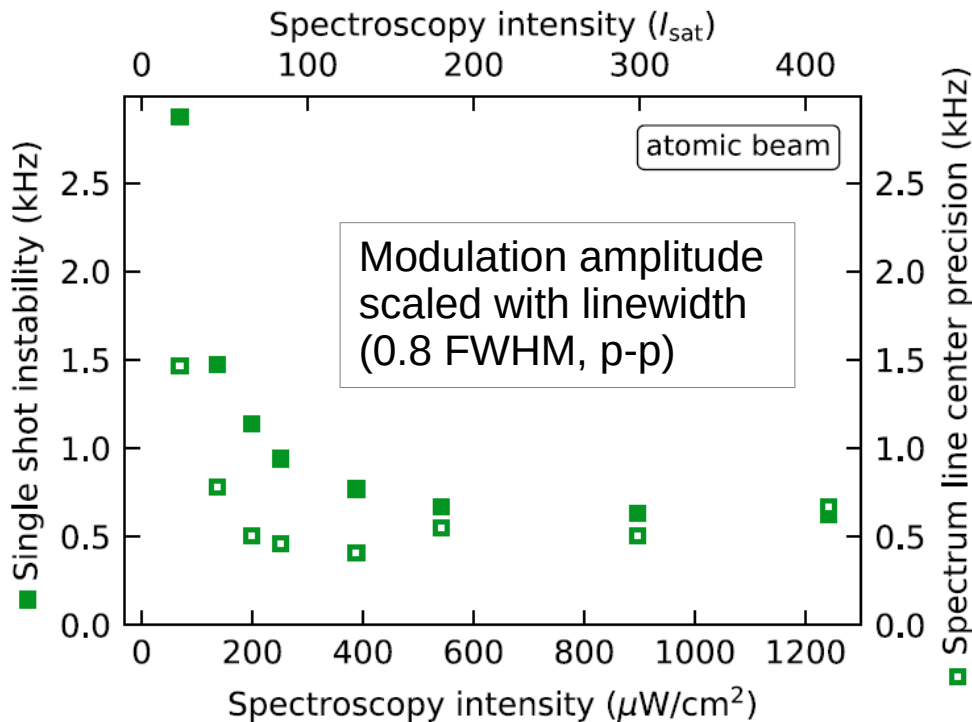
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Frequency instability:

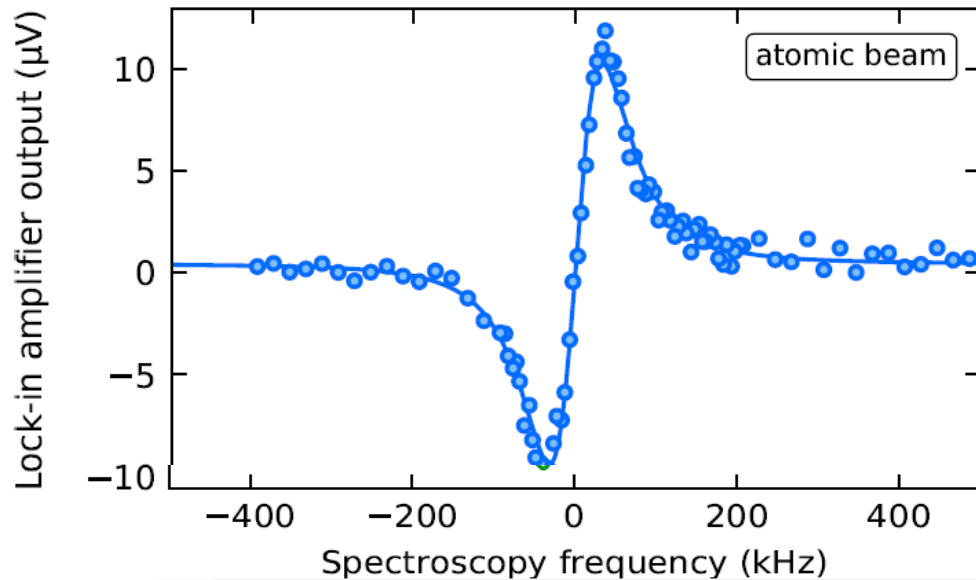
Lowest when power-broadening dominates over transit broadening

High intensities: baseline drifts and lineshape distortion

Optimal at 100 I_{sat} ;

Fit precision statistically consistent with the short-term instability and the sampling

Performances – atomic beam



Lock-in amplifier integration time 1s

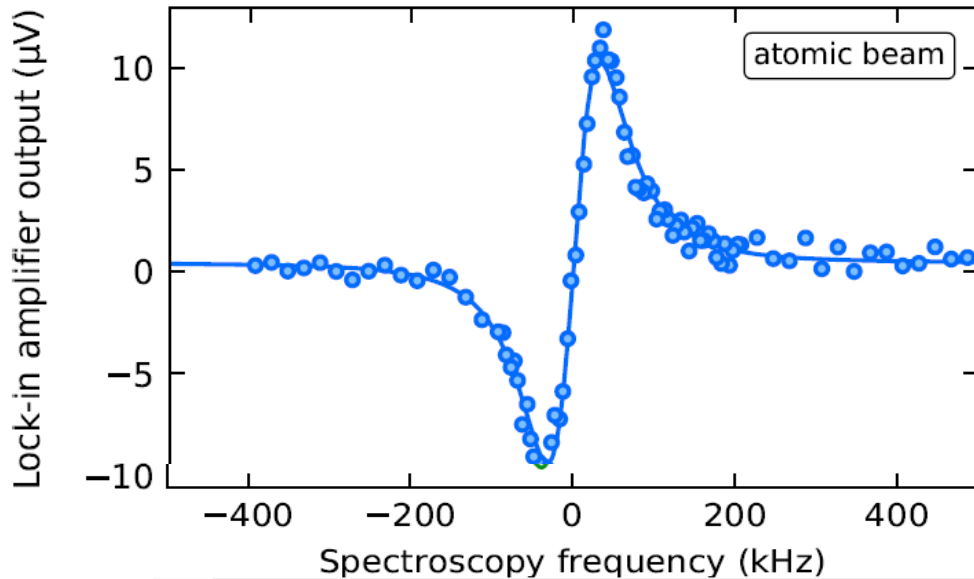
Frequency instability at 1s (1-shot) : 1,2 kHz

Relative freq instability at 1s: $2 \cdot 10^{-12}$

Fit uncertainty 450 Hz

(statistically consistent with the sampling)

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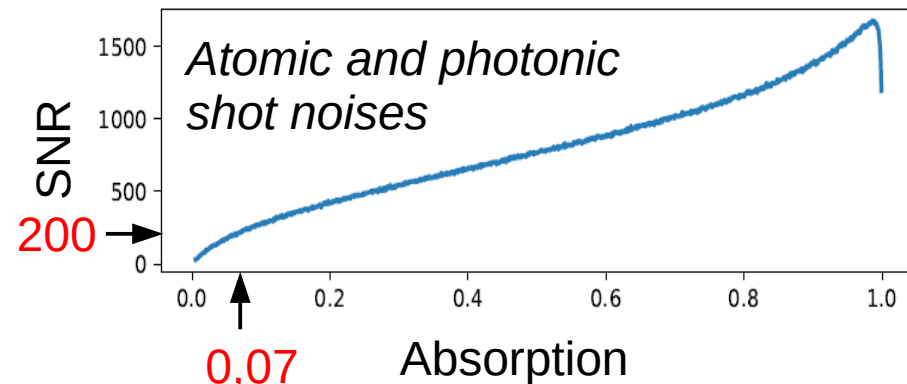
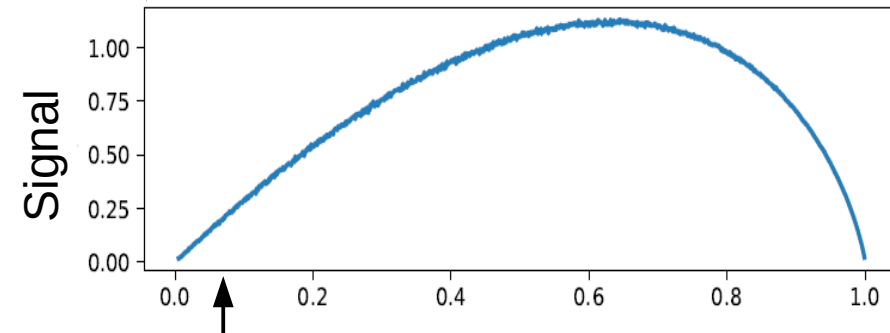
Technically limited performances;
what could be the fundamental limit?

SNR (thus also instability) a factor 10 behind
atomic shot noise limitation : $2 \cdot 10^{-13}$ at 1s

Spectrum at only 7% readout absorption
Very strong improvement achievable by reaching
to **high densities : $3 \cdot 10^{-14}$ at 1s**

Very similar to Ca-beam clocks,
e.g. McFerran 2009: $7 \cdot 10^{-14}$ at 1s

Theoretical estimates



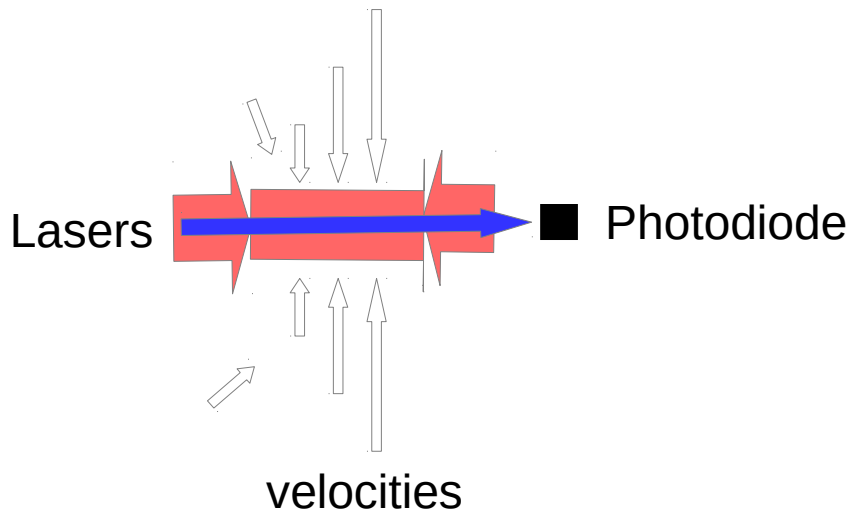
Applicability to a hot cell

Lineshape robustness:

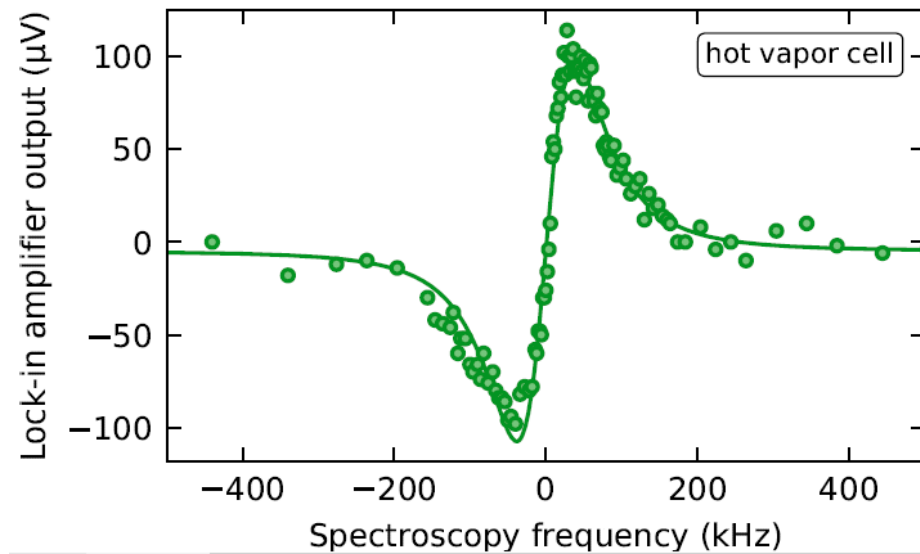
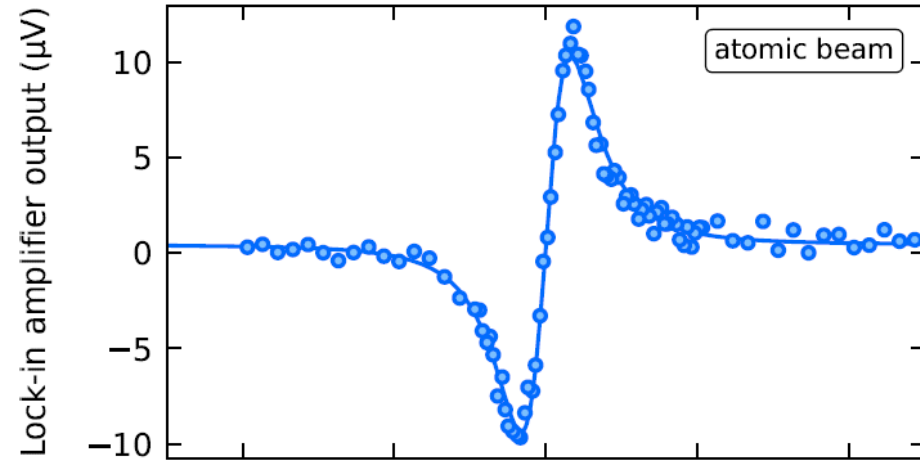
Typical transit time $8 \mu\text{s} \ll 1/\gamma = 21 \mu\text{s}$:
coherent evolution.

The shape still remains close to Lorentzian,
due to **velocity averaging**

→ **strong stability of the lineshape with I**



Reproduction of the same spectrum,
at same I/I_{sat} .



Applicability to a hot cell

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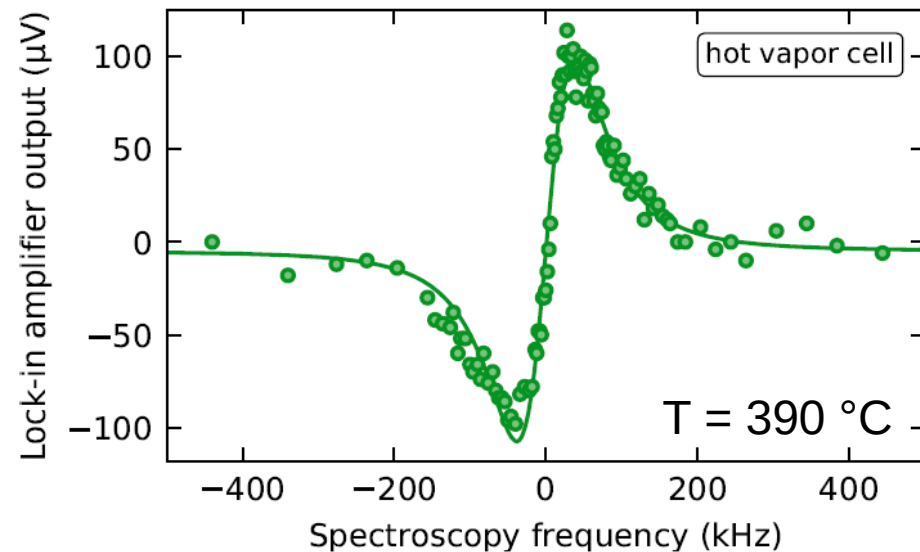
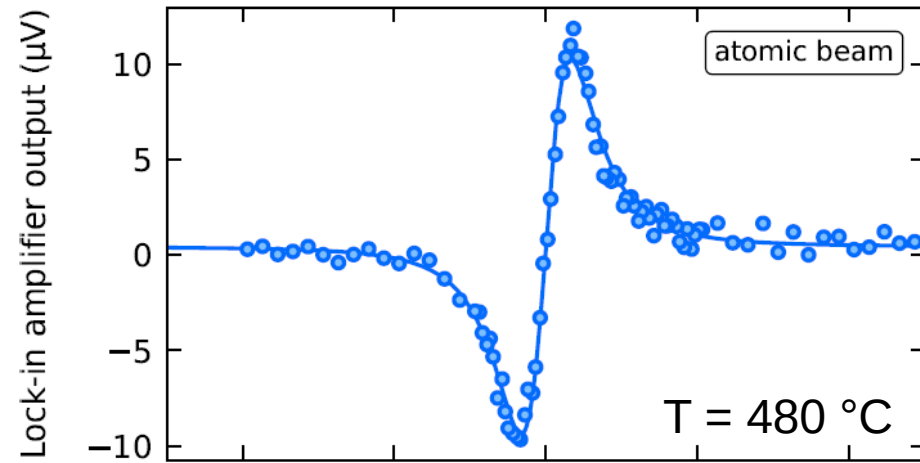
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Compactness and source lifetime:

- No signal degradation nor shift vs pressure up to 10^{-3} mbar of Argon: **no need for pump**
- Absorption 80% despite 100K lower temperature

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Robust against first order Doppler shift

spectroscopy

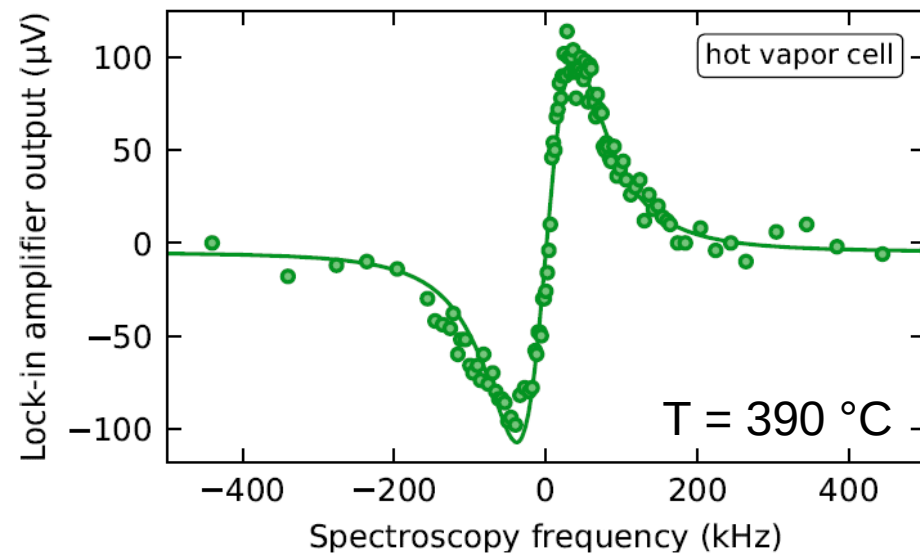
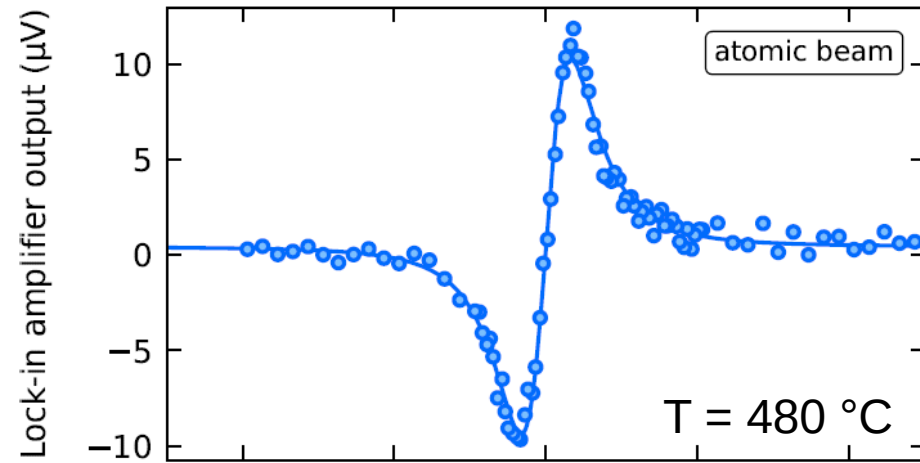


$$\vec{k}_1 \cdot \vec{v} = \vec{k}_2 \cdot \vec{v} \neq 0$$

Atoms

Beam : $50 \mu\text{rad} \rightarrow 10 \text{ kHz shift (and similar broadening)}$
Cell: symmetric velocity distribution \rightarrow only broadening

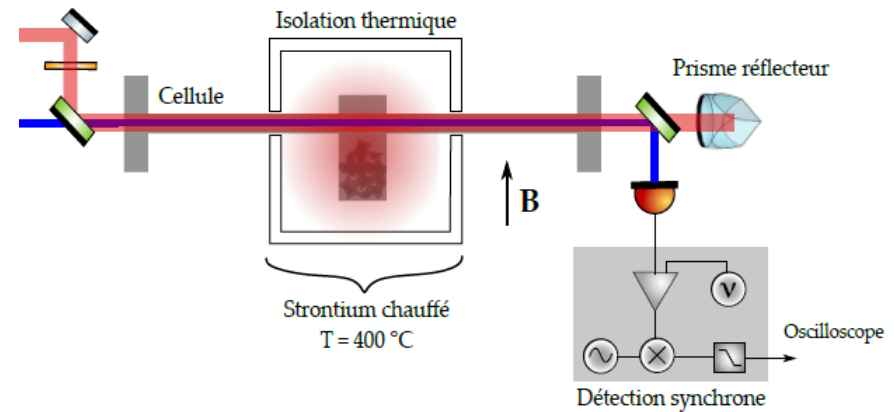
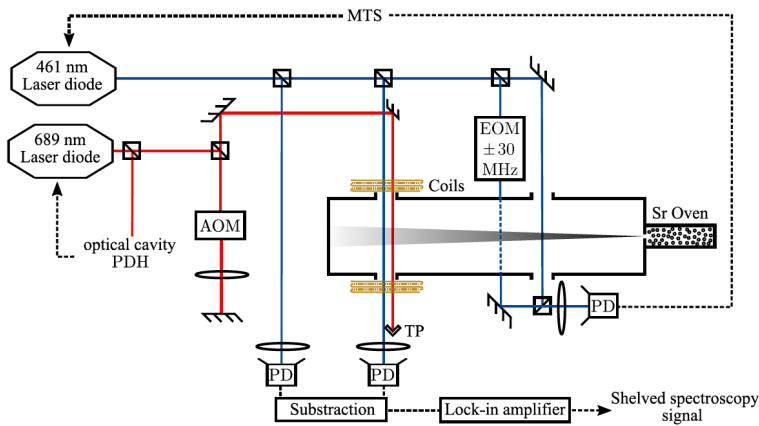
Reproduction of the same spectrum,
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Concluding remarks

A robust solution, demonstrated on two fully independent setups:
Atomic beam with separated interrogation zone,
and
Hot cell with overlapping beams

ArXiv:1910.11718

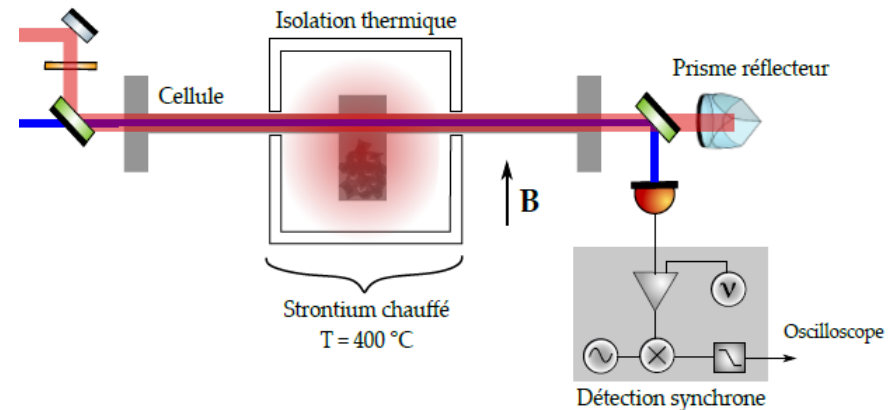
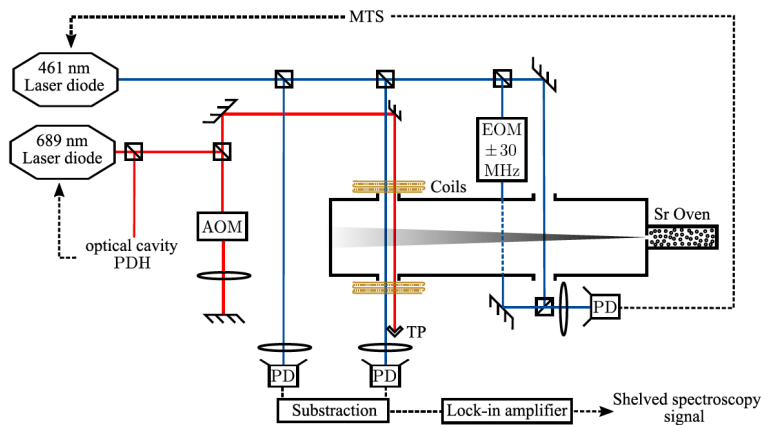


Shelving detection easily applicable to all strontium experiments

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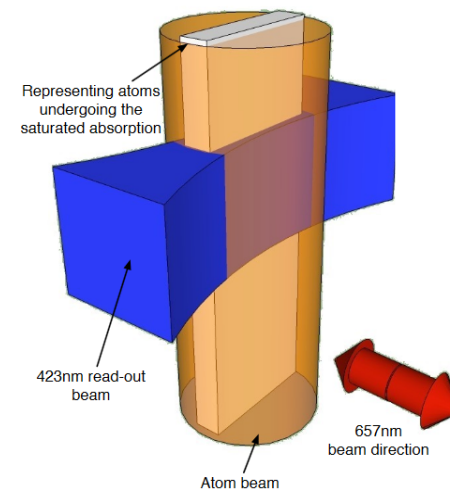


Shelving detection easily applicable to all strontium experiments

A reference of metrological interest?

- short-term instability: achieved $2 \cdot 10^{-12}$ at 1s (beam setup)
achievable $3 \cdot 10^{-14}$ at 1s with same setup
- perspectives similar to Ca-beam clocks, as low-cost clock
[Kürzig group project: a transportable Sr Ramsey clock]

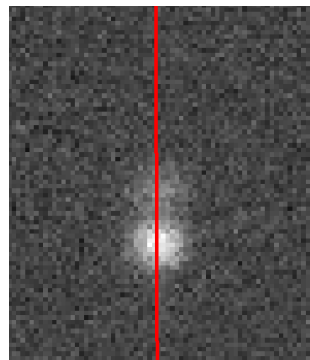
Many ideas of Ca-beam clocks should be identically applicable
(Mc Ferran 2009, Shang 2017)



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→ applicable to most Sr experiments

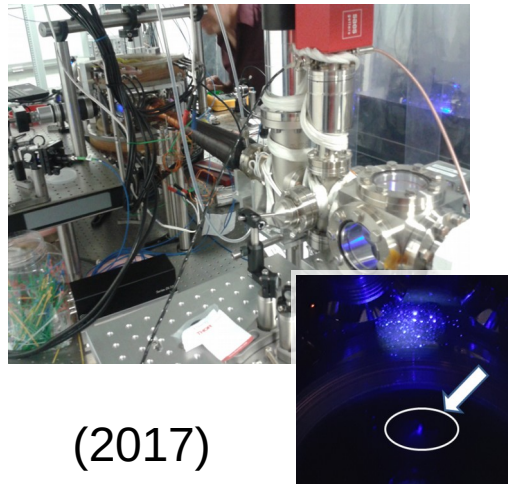
[ArXiv:1910.11718](https://arxiv.org/abs/1910.11718)

- 2) Birth of the Strontium experiment
 - a degenerate Fermi gas with 10 spin-states
 - first experiments of coherent spin manipulation



Spin-dependent adiabatic momentum transfer

Birth of the strontium experiment



Blue MOT (1 mK)
461 nm
30 MHz

$5s^2\ ^1S_0$

$5s5p\ ^1P_1$

$5s4d\ ^1D_2$

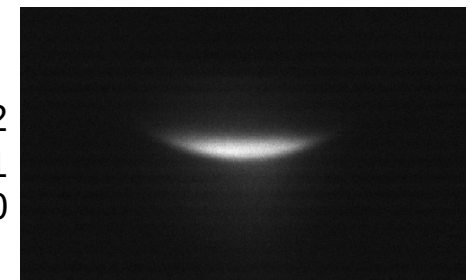
$5s5p\ ^3P_j$
J = 2
J = 1
J = 0

$5s6d\ ^3D_j$

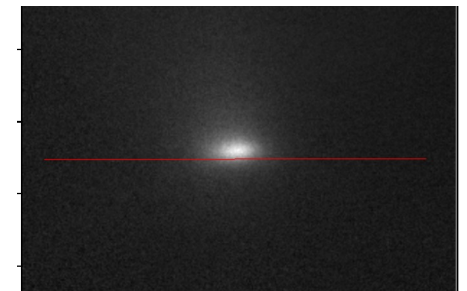
J = 3
J = 2
J = 1

Repumping
403 nm

^{88}Sr (May 2018)



^{87}Sr



Red MOT (1 μK)
689 nm
7.4 kHz

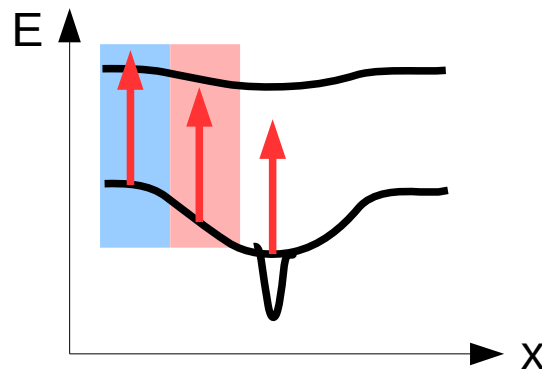
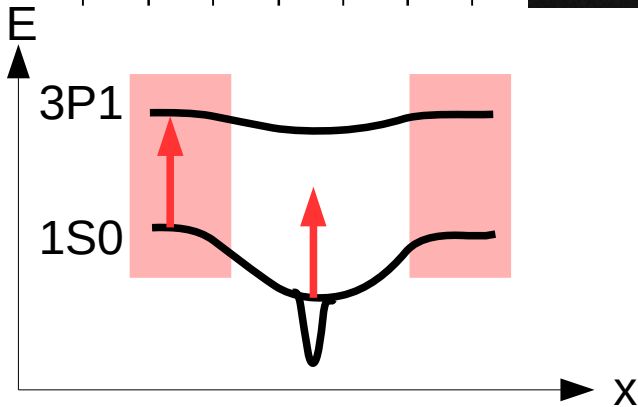
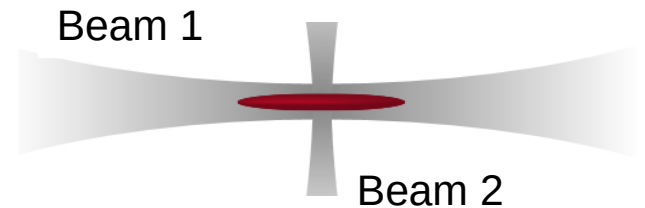
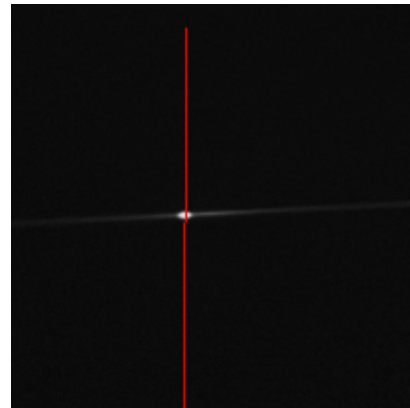
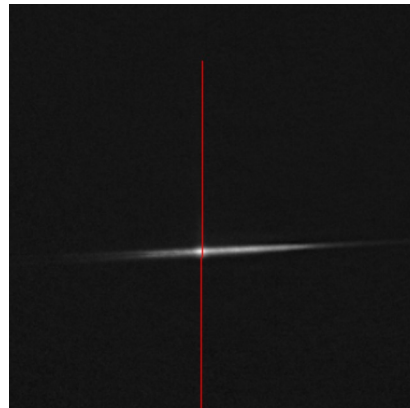
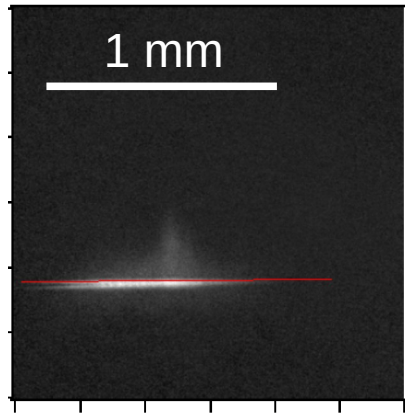
1:50 000

1:3

Cold and dense: in principle ideal for loading an optical trap

Birth of the strontium experiment

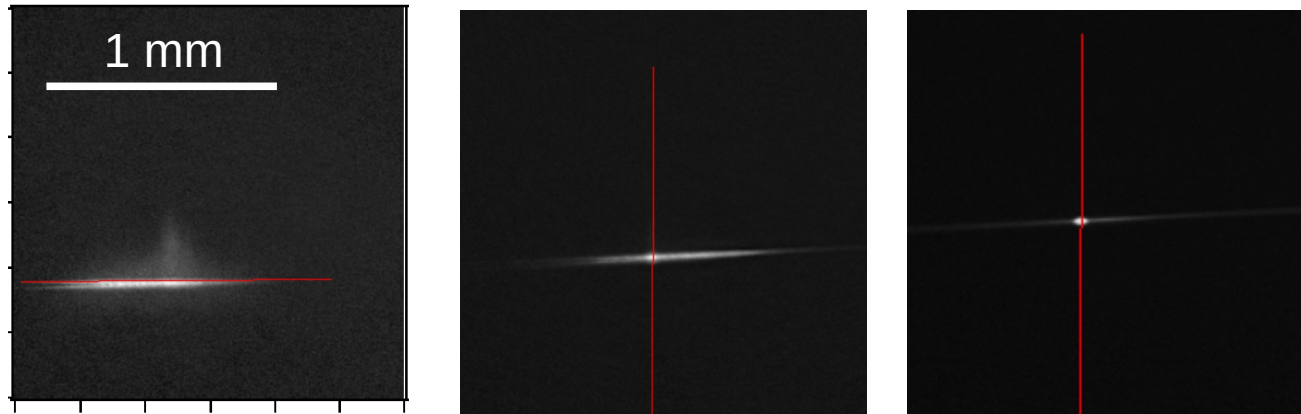
Laser cooling in light shifts from the dipole trap $O(100 \text{ kHz})$
 $3 \mu\text{K}$



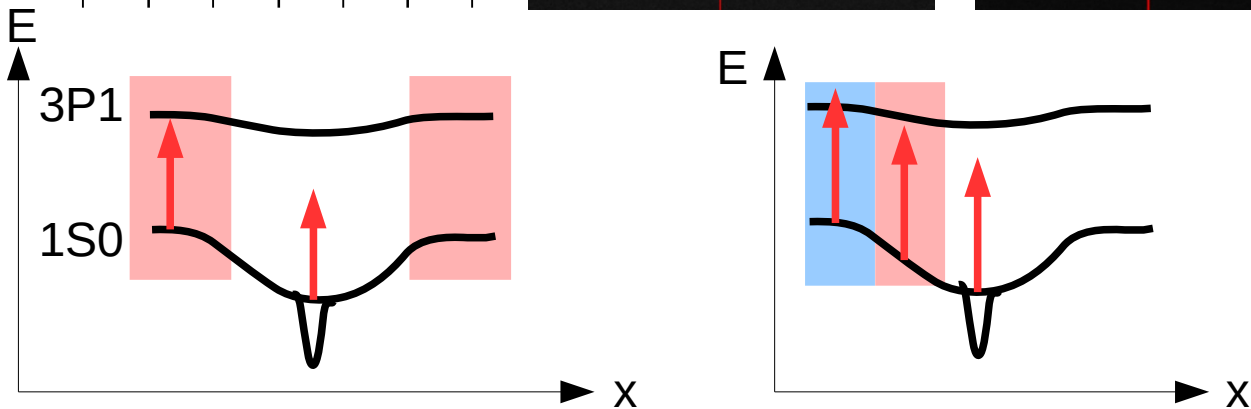
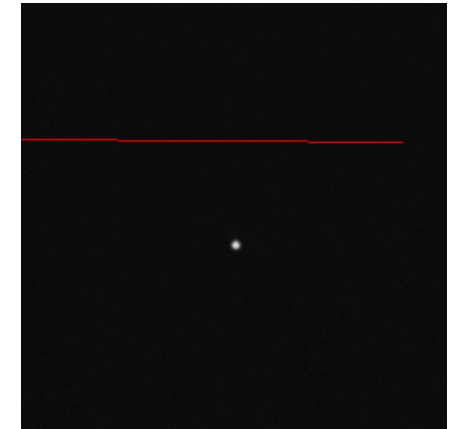
**Loading stage sensitive to frequency drifts by $O(10 \text{ kHz})$:
stable referencing essential**

Birth of the strontium experiment

Laser cooling in light shifts from the dipole trap $O(100 \text{ kHz})$
 $2 \mu\text{K}$

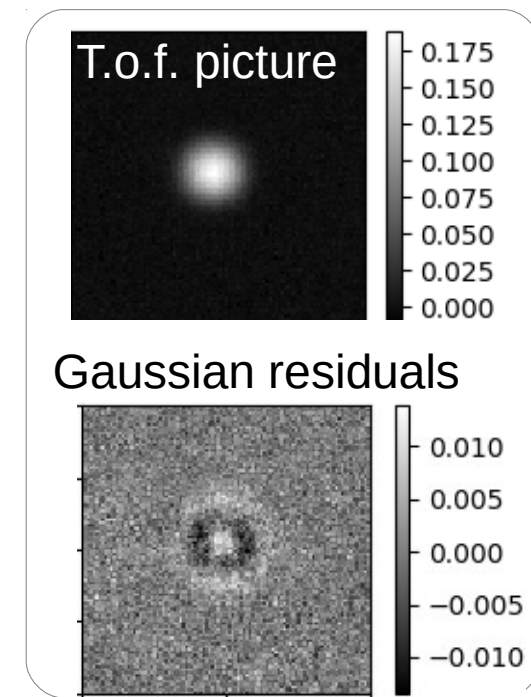


Evaporation



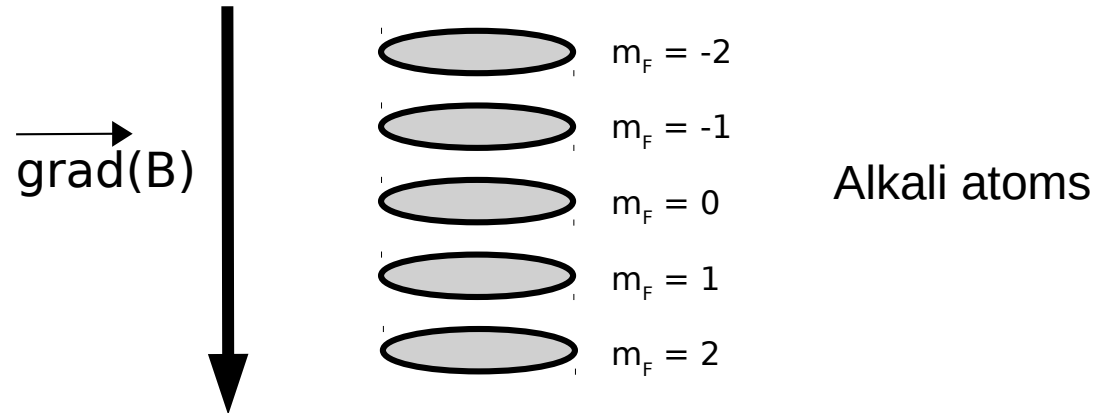
**Loading stage sensitive to frequency drifts by $O(10 \text{ kHz})$:
stable referencing essential**

Since spring 2019 : Fermi gas with 10 spin states,
down to $T/T_f \sim 0,2$

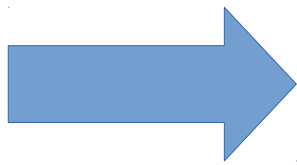


Spin state measurement

- Stern-Gerlach separation,
+ broad line imaging ?



Impossible because of very small (purely nuclear) magnetic dipole moment.



How to spatially separate the spin states,
before imaging on the broad line?

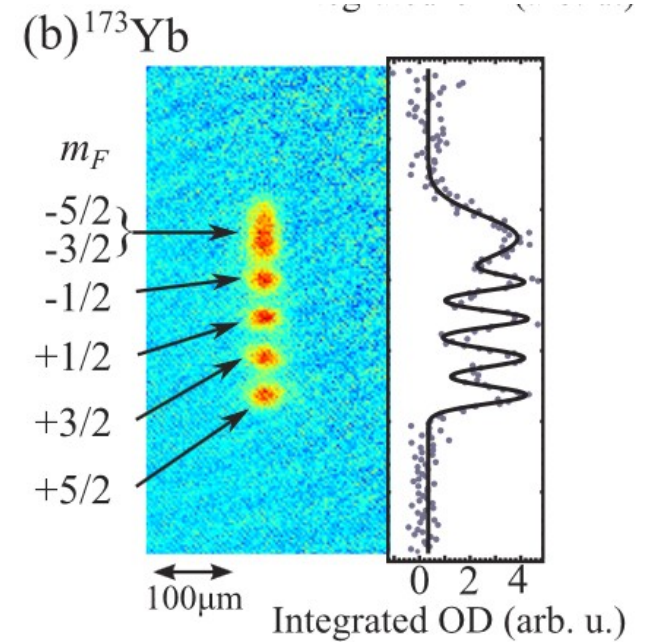
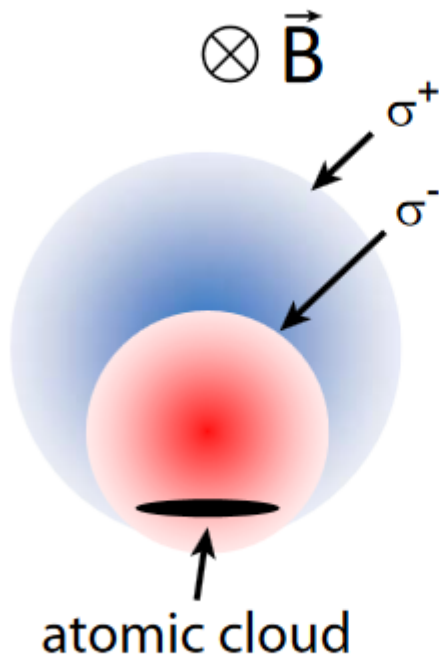
Spin state measurement

Established technique in this spirit:
Optical Stern-Gerlach separation

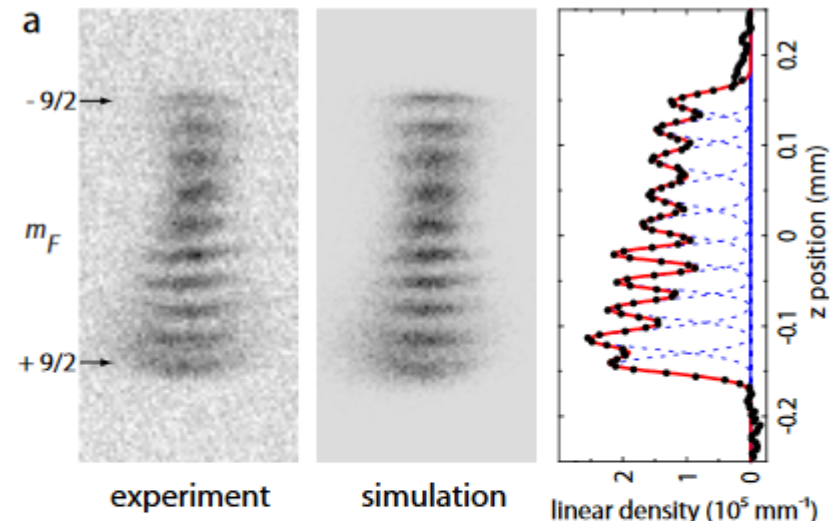
large gradients of spin-dependent light shifts
applied for $\sim 1\text{ms}$

Requires specific lasers and beamshapes

**We present an alternative scheme that
simply relies on the narrow-line MOT beams**



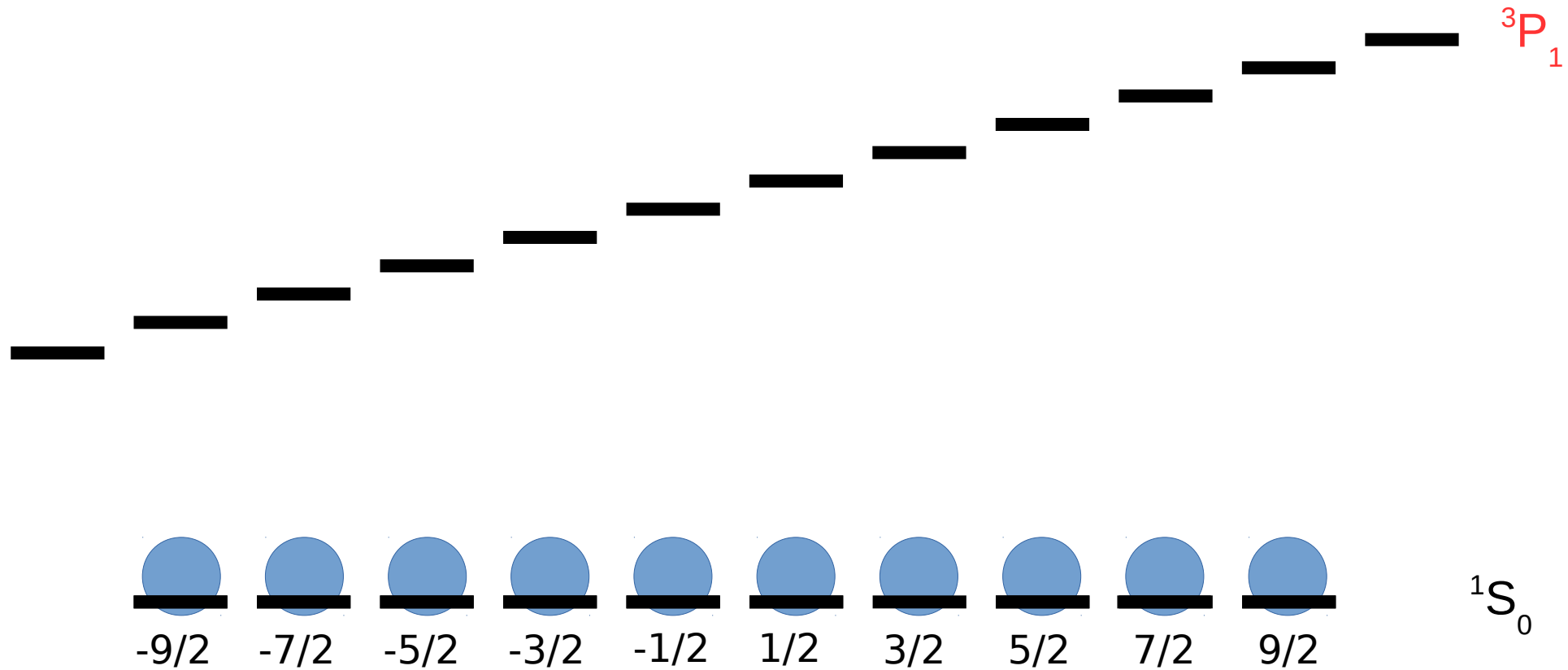
Yb: Taie 2010, Phys. Rev. Lett. 105, 190401



Sr: Stellmer 2011, Phys. Rev. A 84, 043611

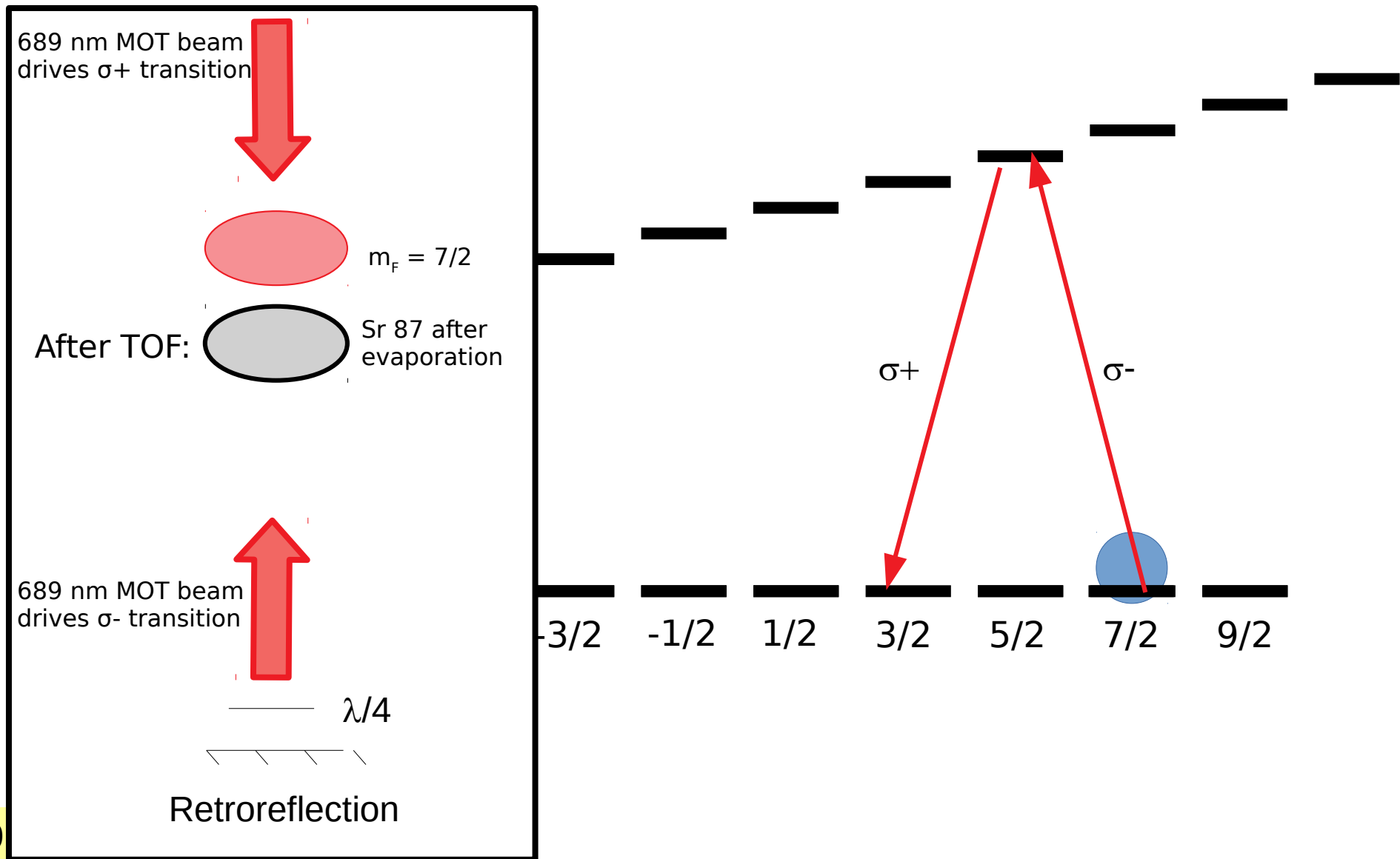
Spin state measurement

Spin-dependent momentum transfer



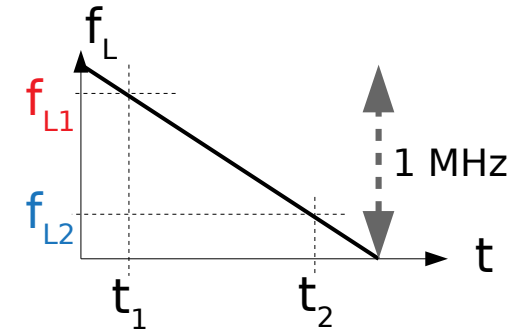
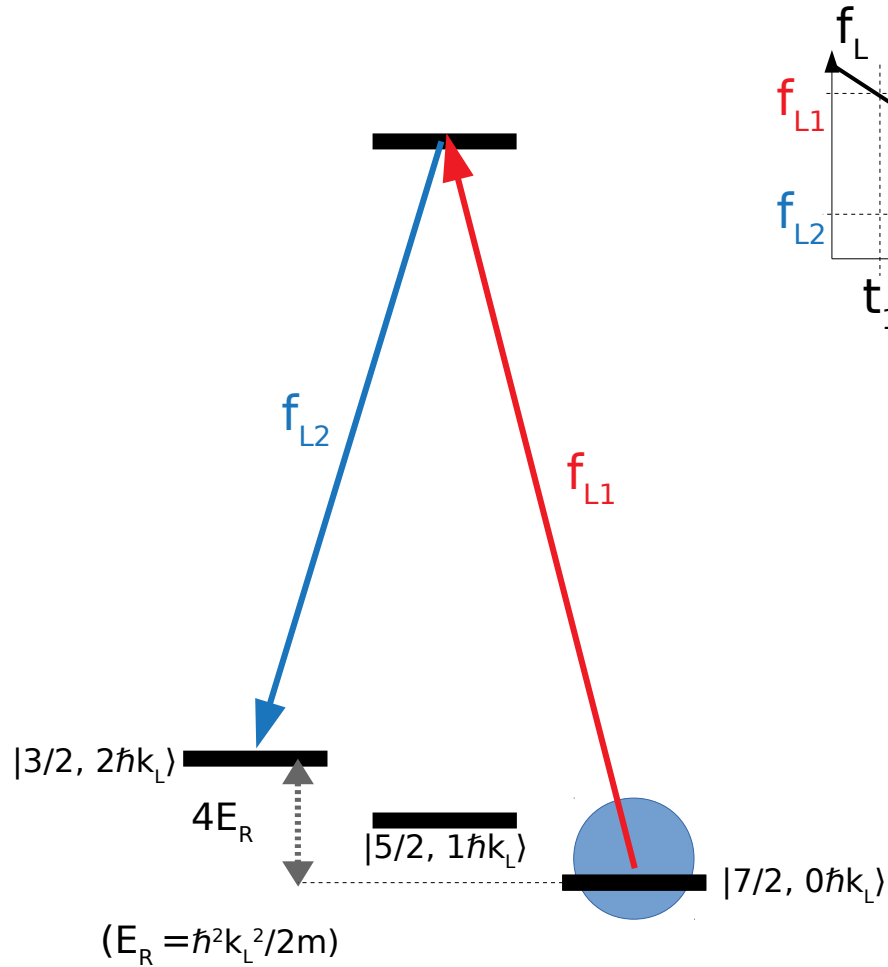
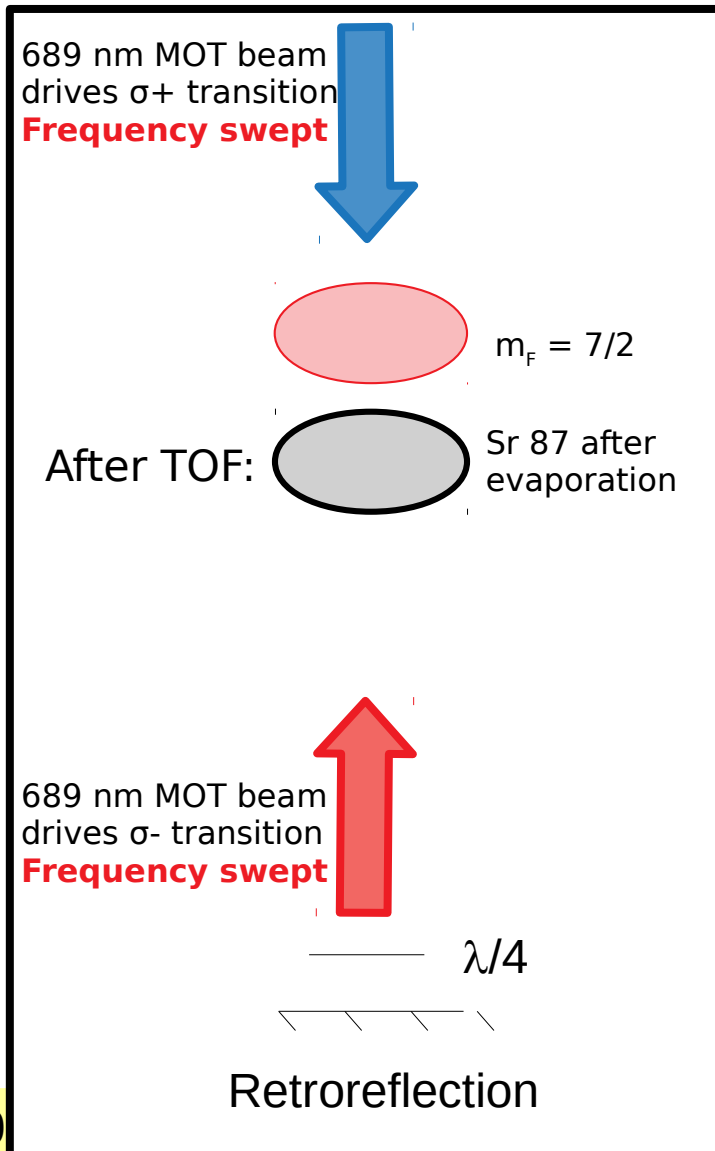
Spin state measurement

Spin-dependent momentum transfer



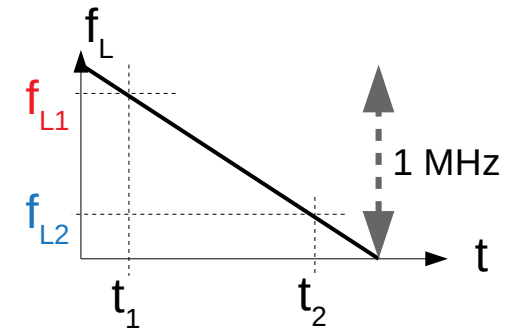
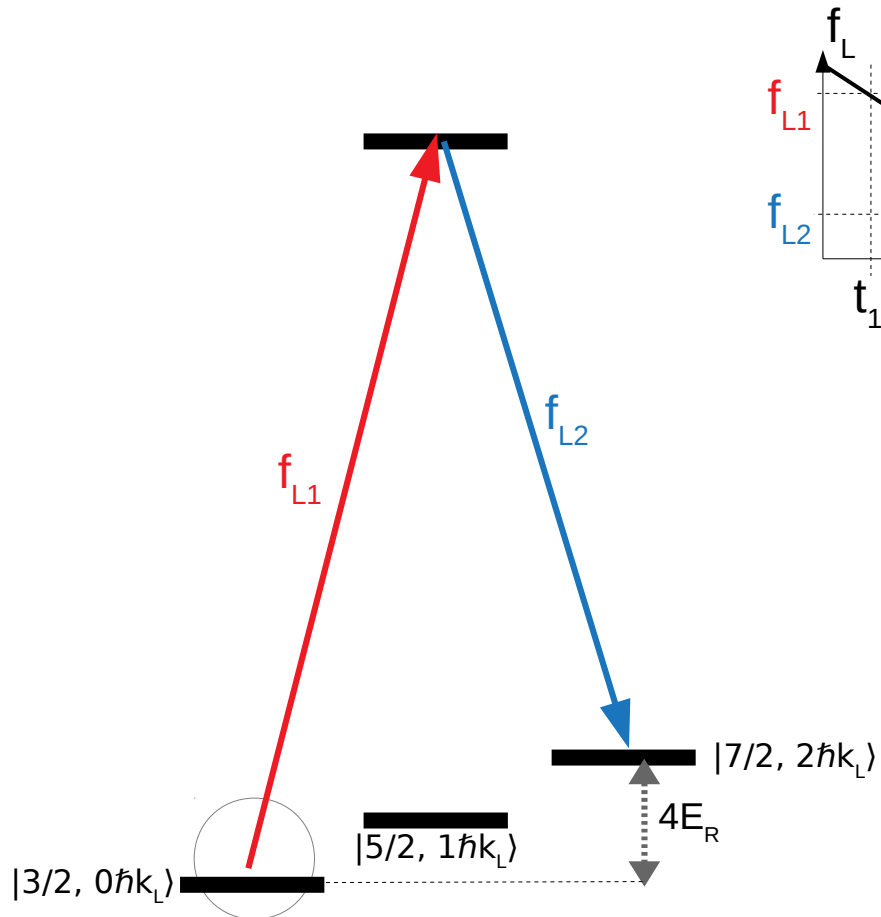
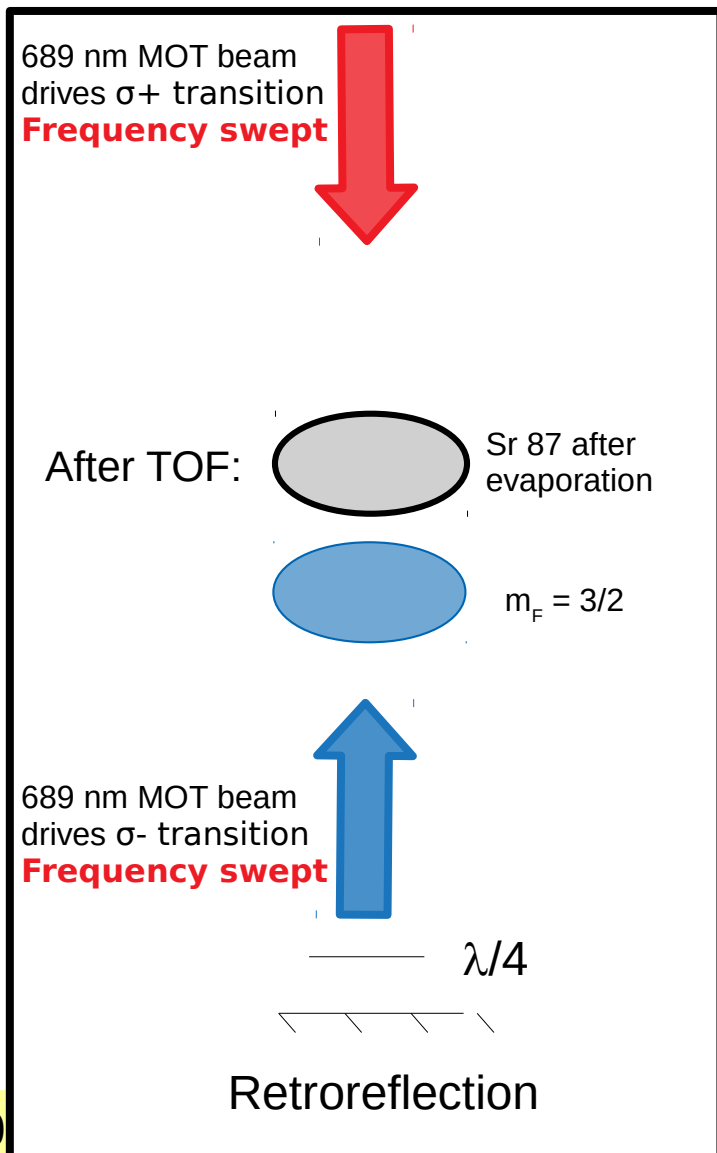
Spin state measurement

Spin-dependent momentum transfer



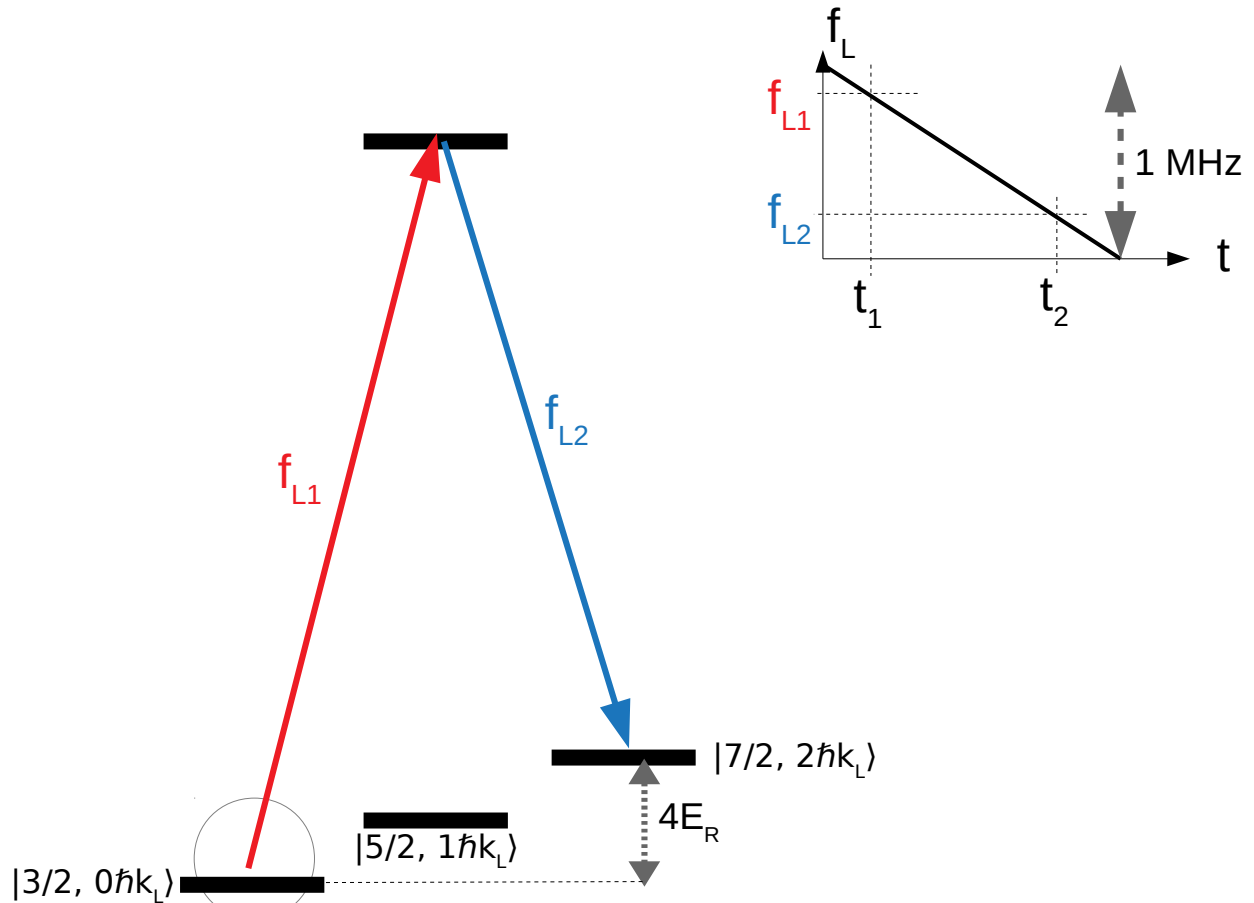
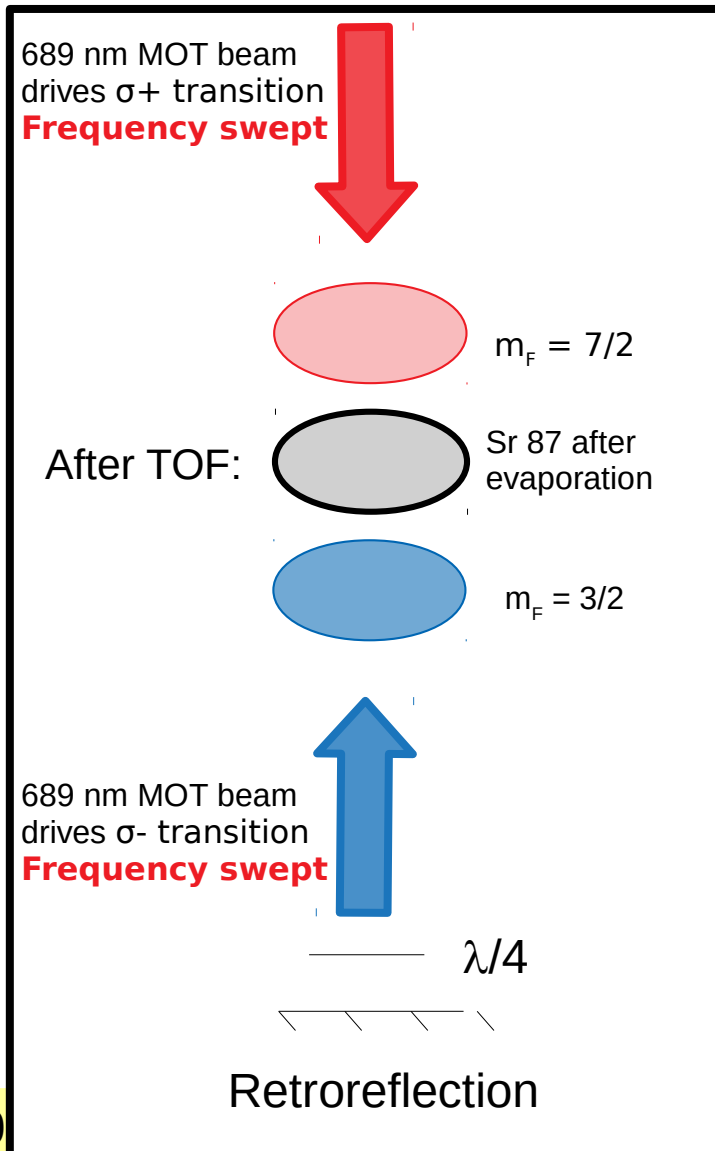
Spin state measurement

Spin-dependent momentum transfer



Spin state measurement

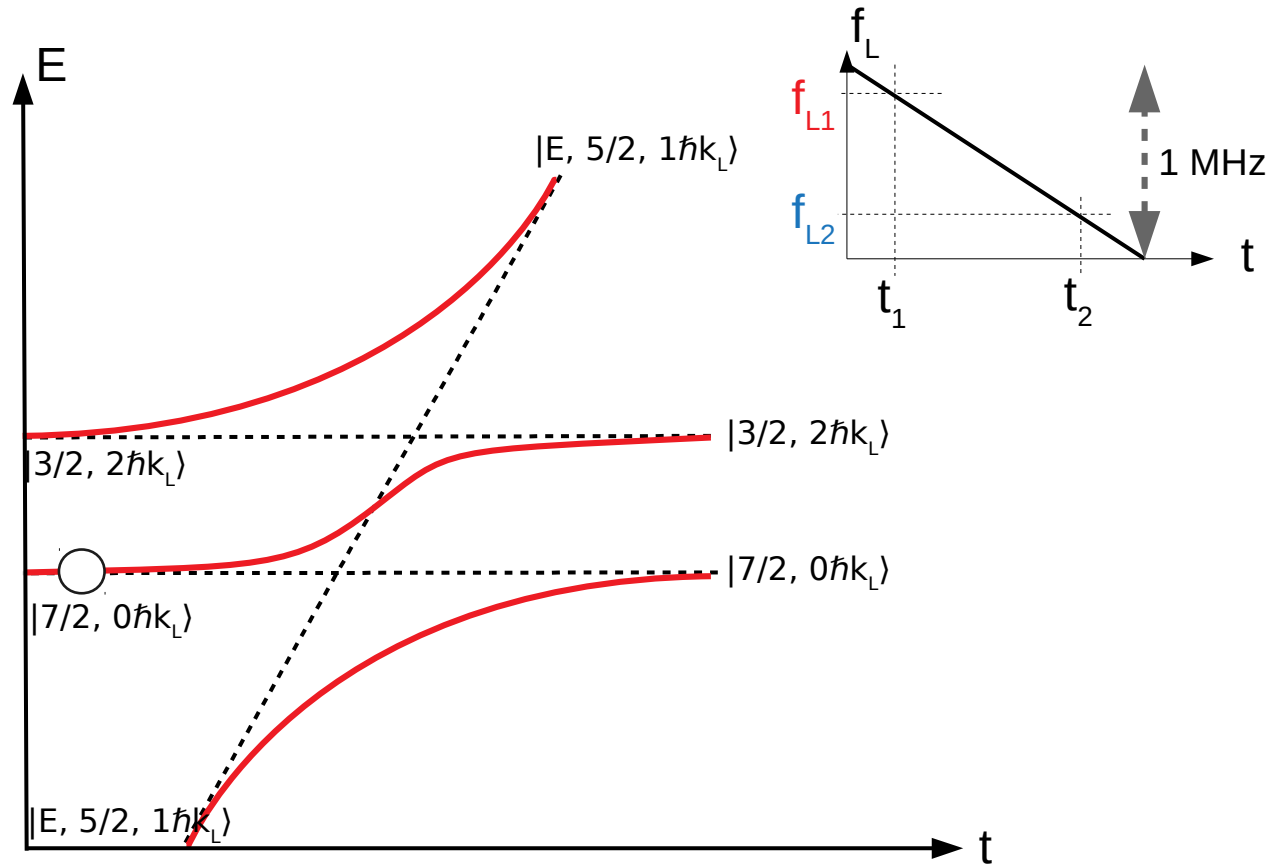
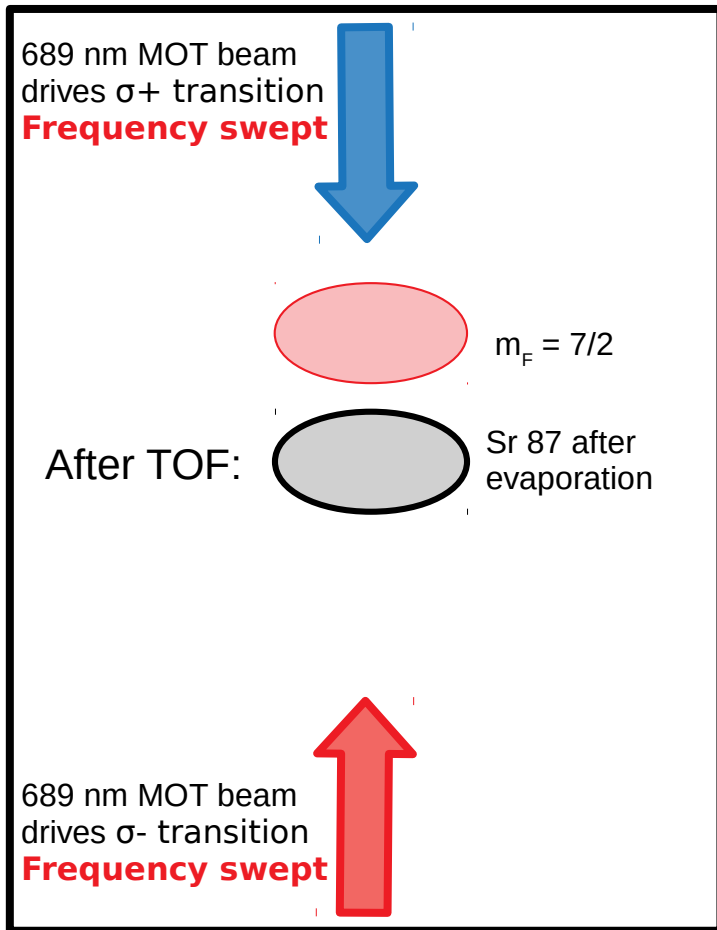
Spin-dependent momentum transfer



Two spin states separated in one run

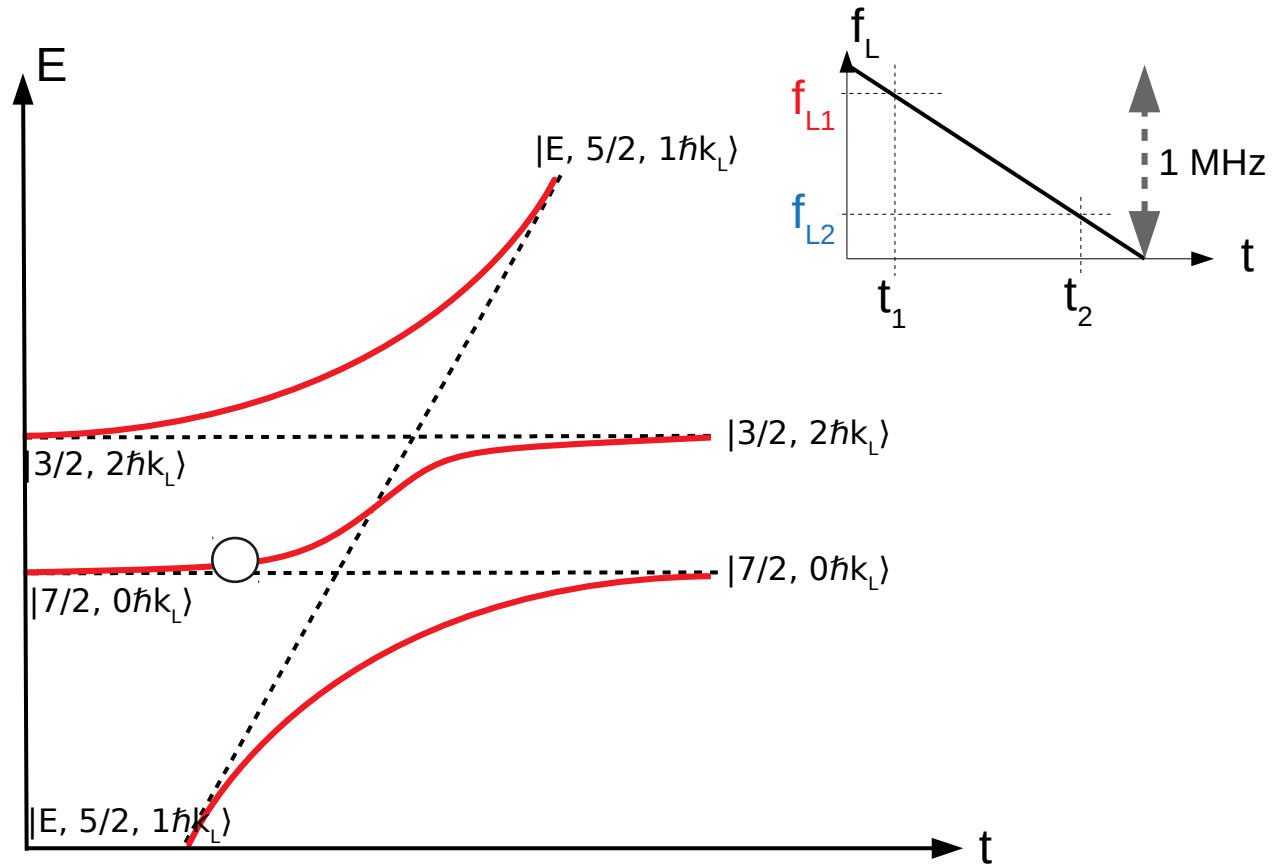
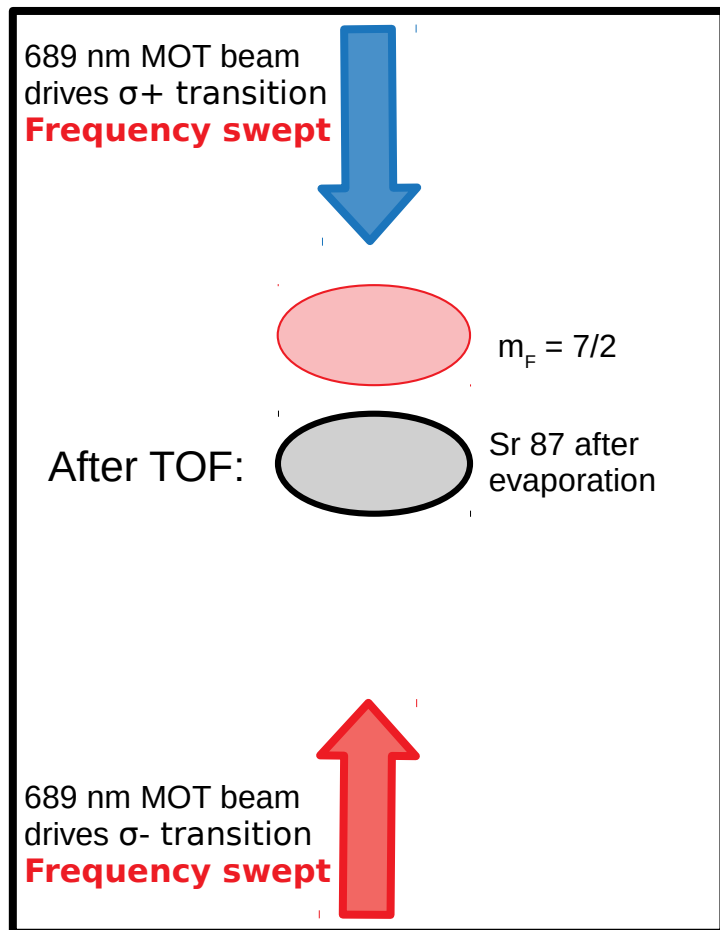
Spin state measurement

Adiabatic spin-dependent momentum transfer



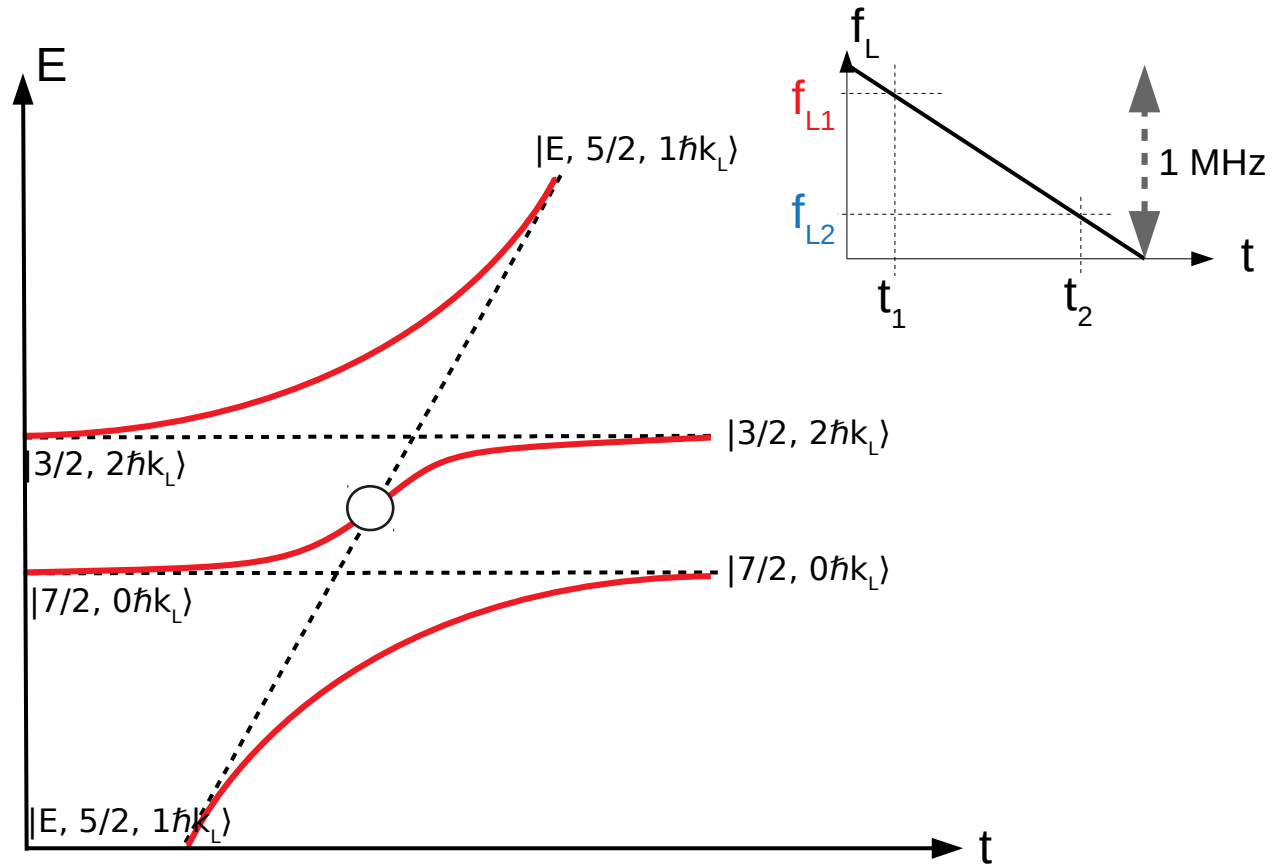
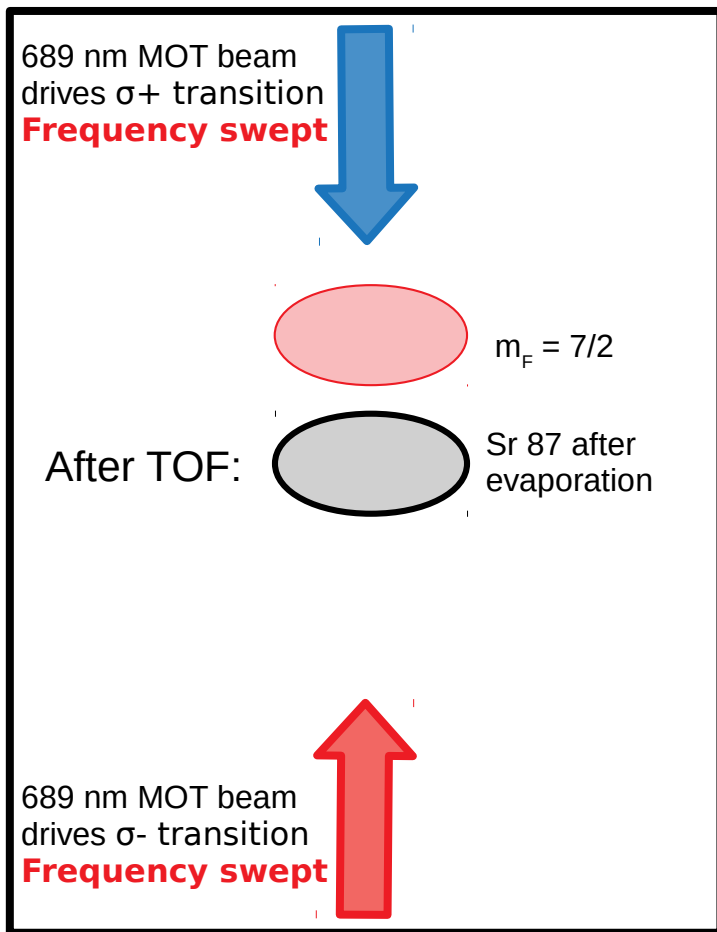
Spin state measurement

Adiabatic spin-dependent momentum transfer



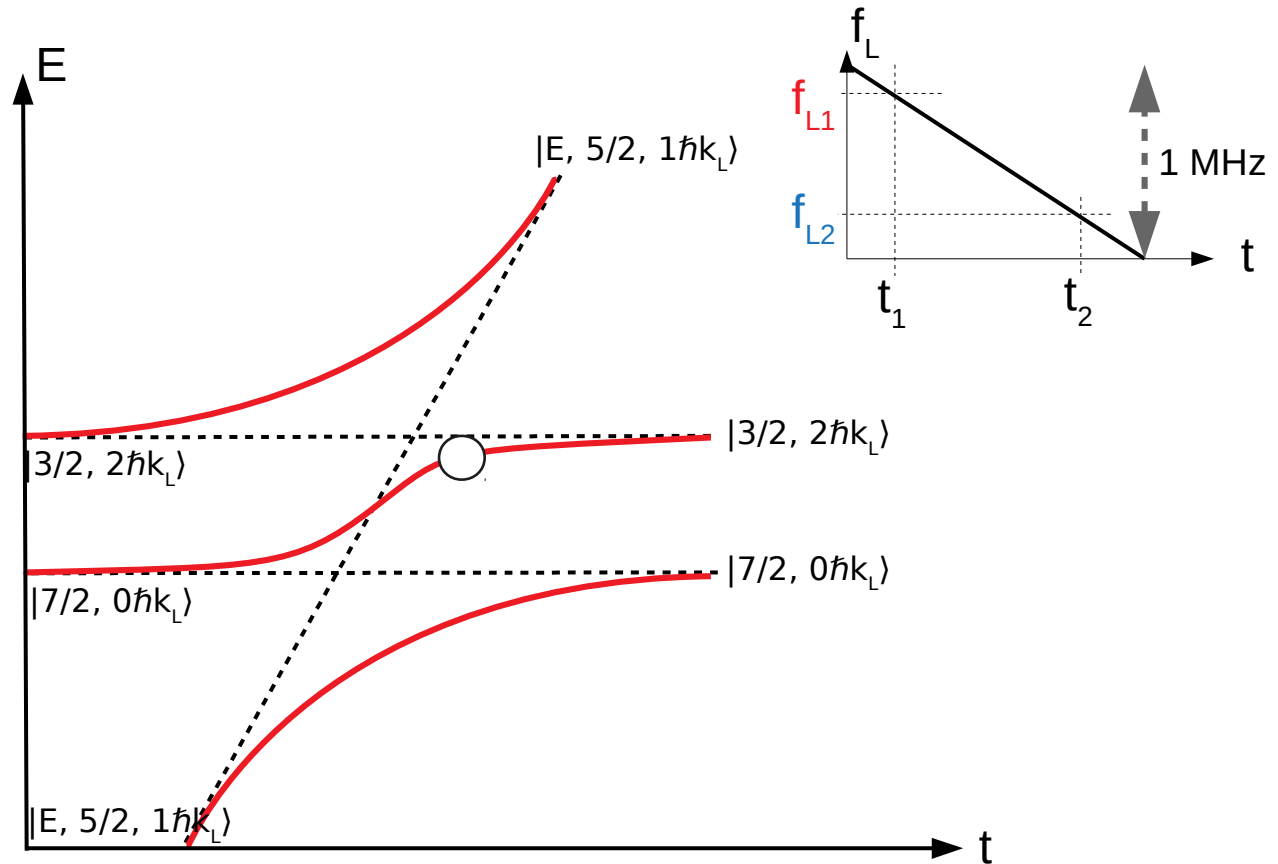
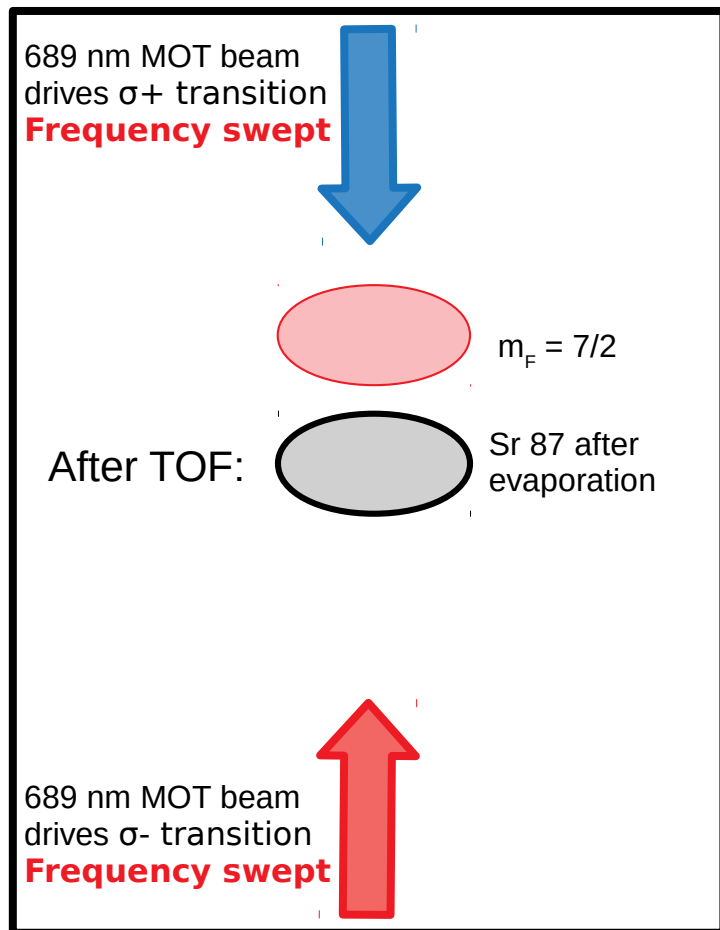
Spin state measurement

Adiabatic spin-dependent momentum transfer



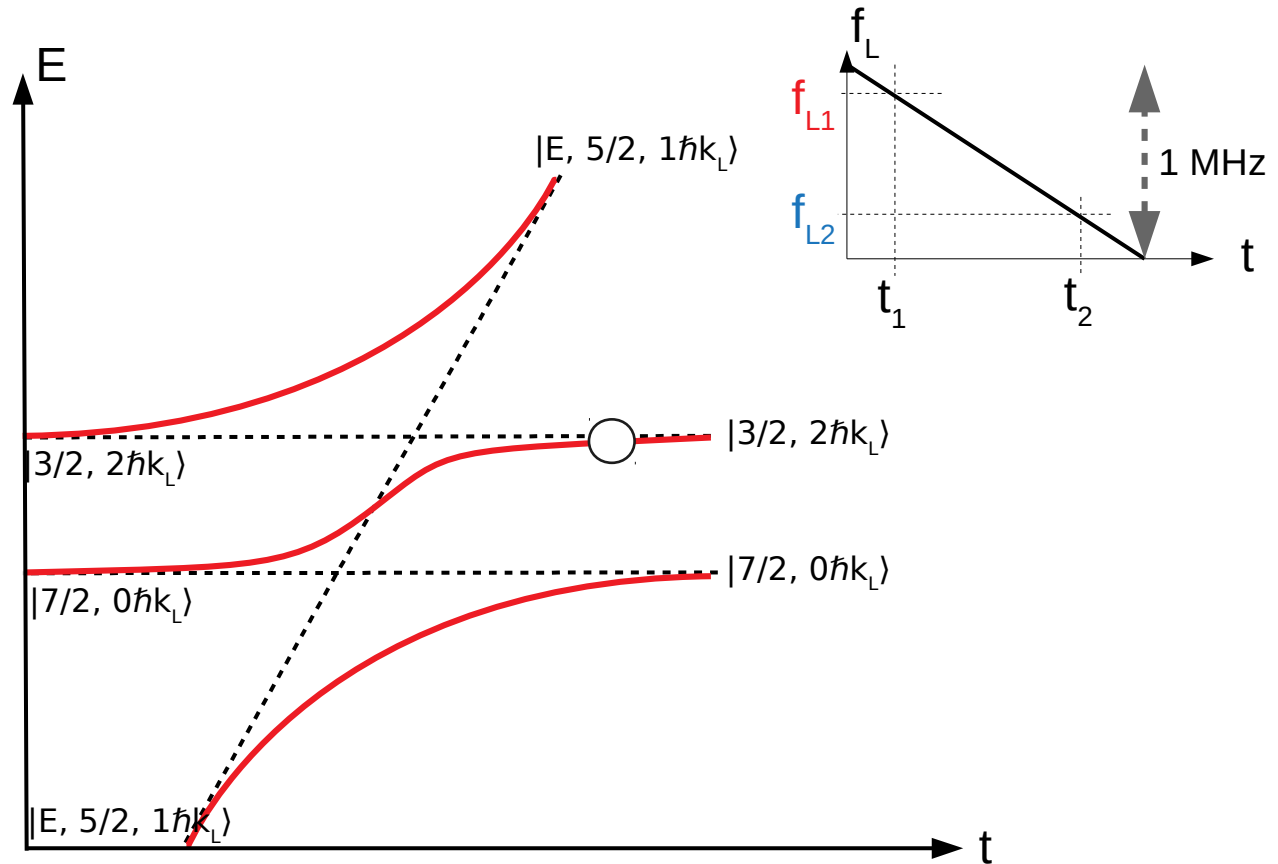
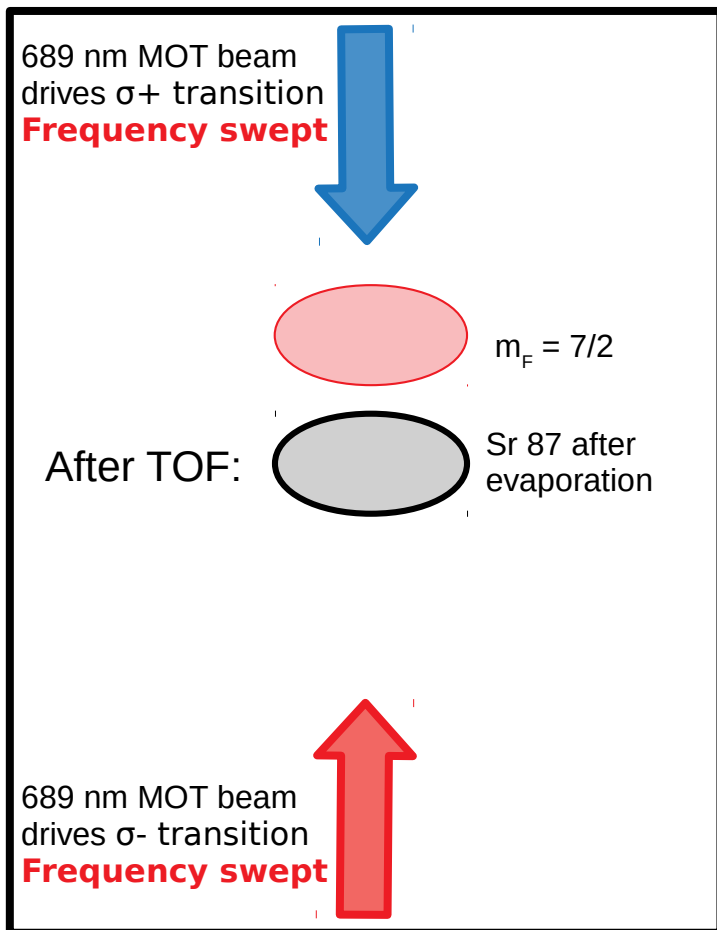
Spin state measurement

Adiabatic spin-dependent momentum transfer



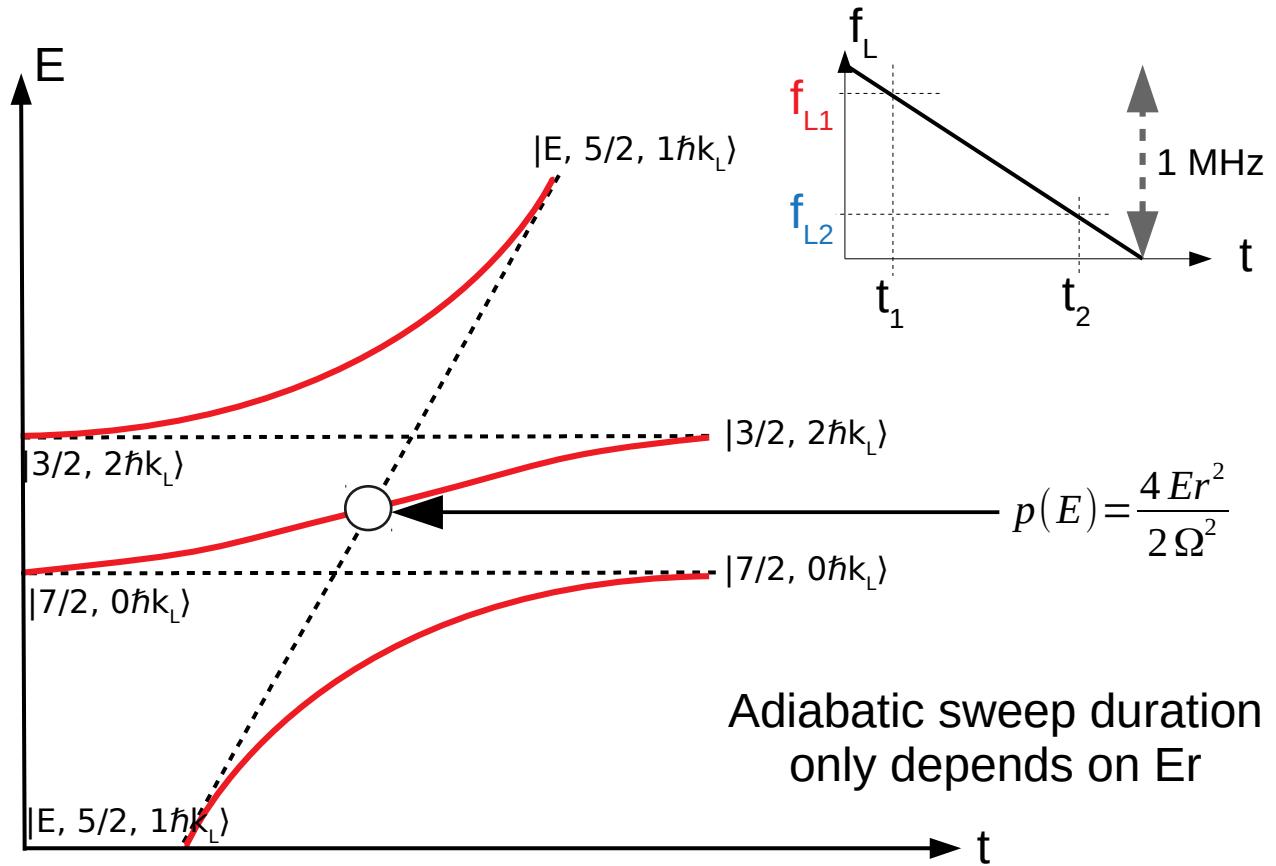
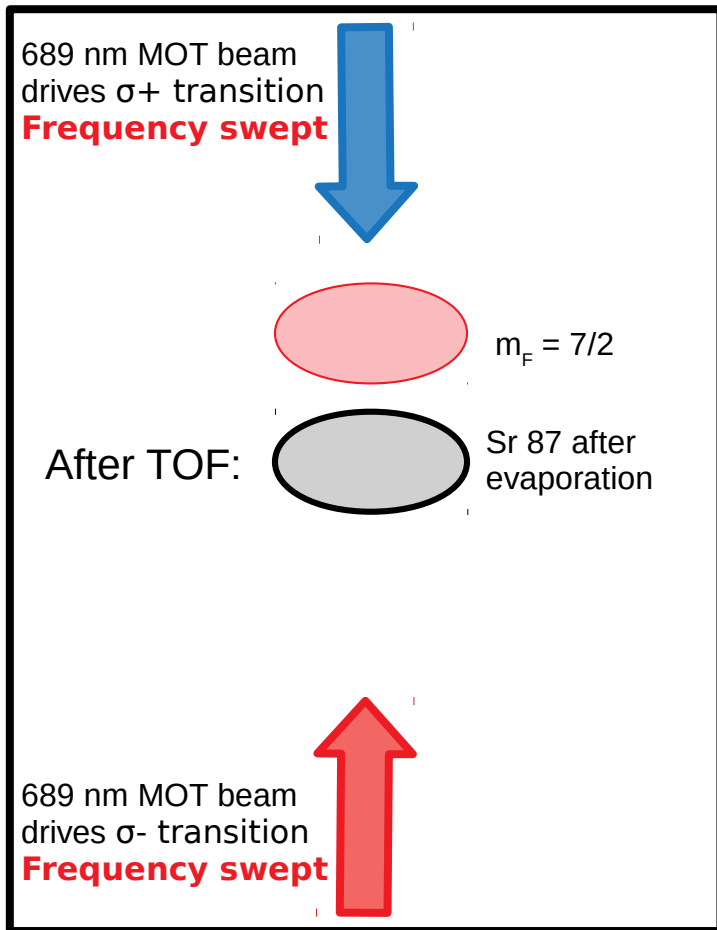
Spin state measurement

Adiabatic spin-dependent momentum transfer



Spin state measurement

Adiabatic spin-dependent momentum transfer

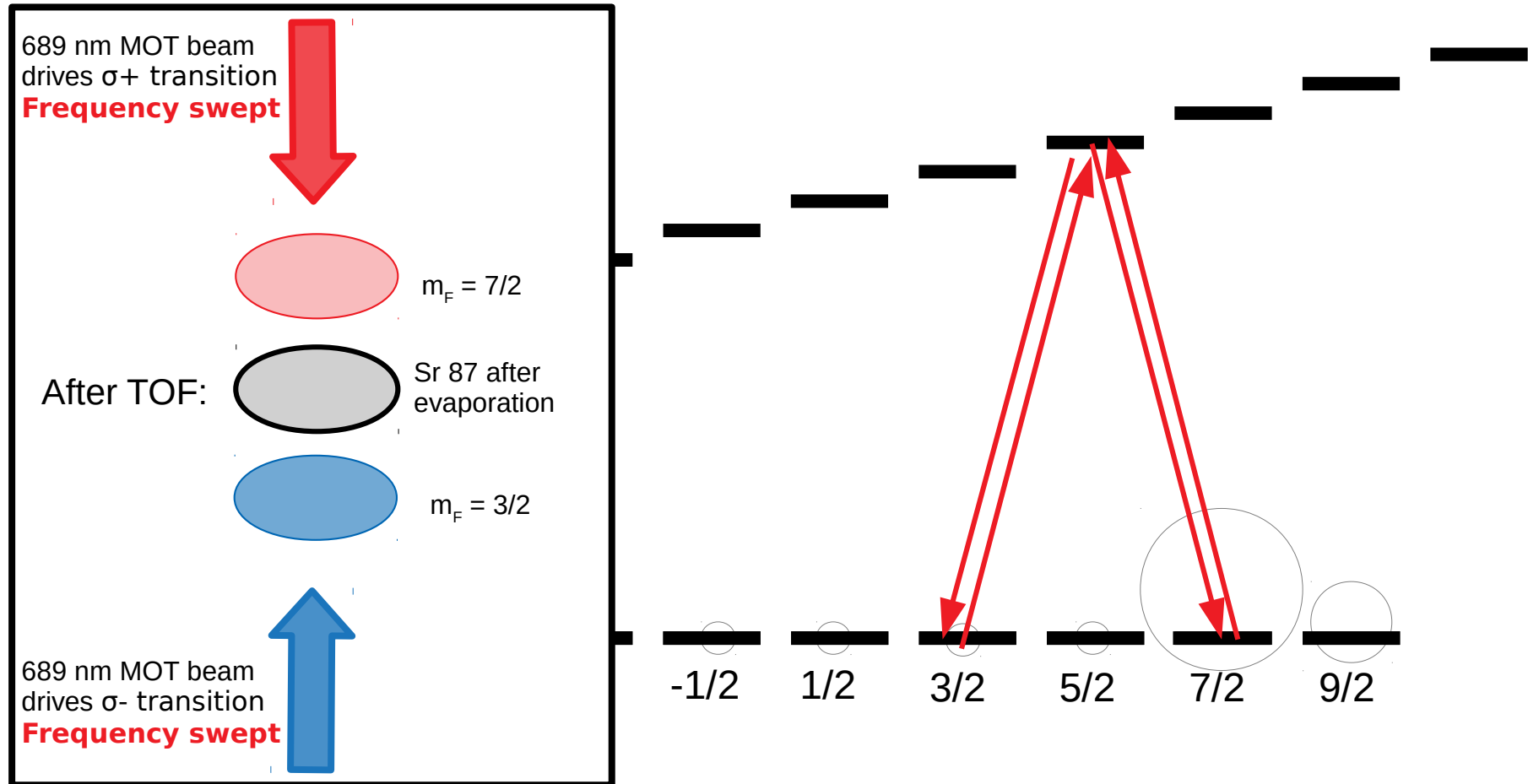


"Grey" adiabatic state:
spontaneous emission strongly suppressed
through the atomic resonance

reminiscent of STIRAP

Spin state measurement

Full population measurements

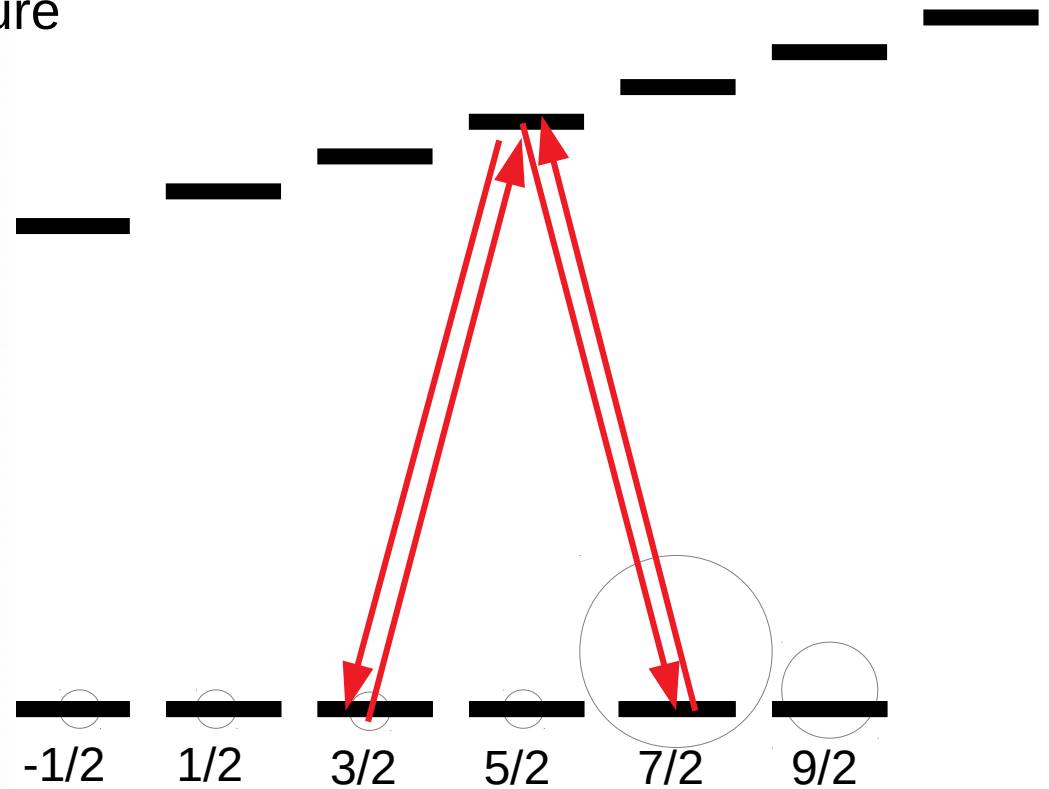
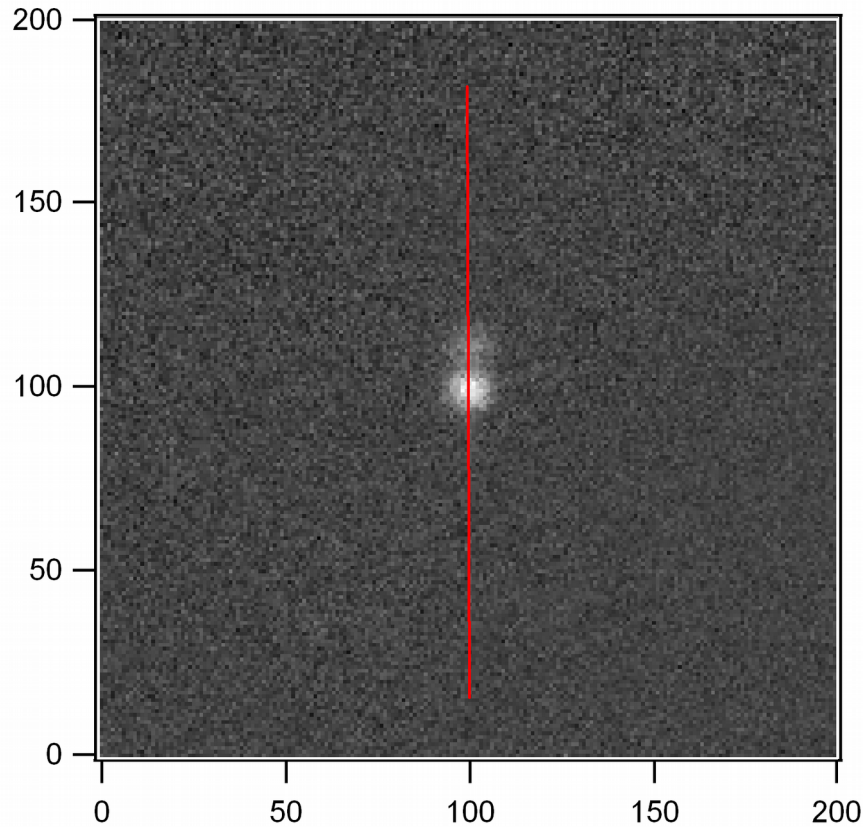


Two spin state populations measured in one run

Spin state measurement

Full population measurements

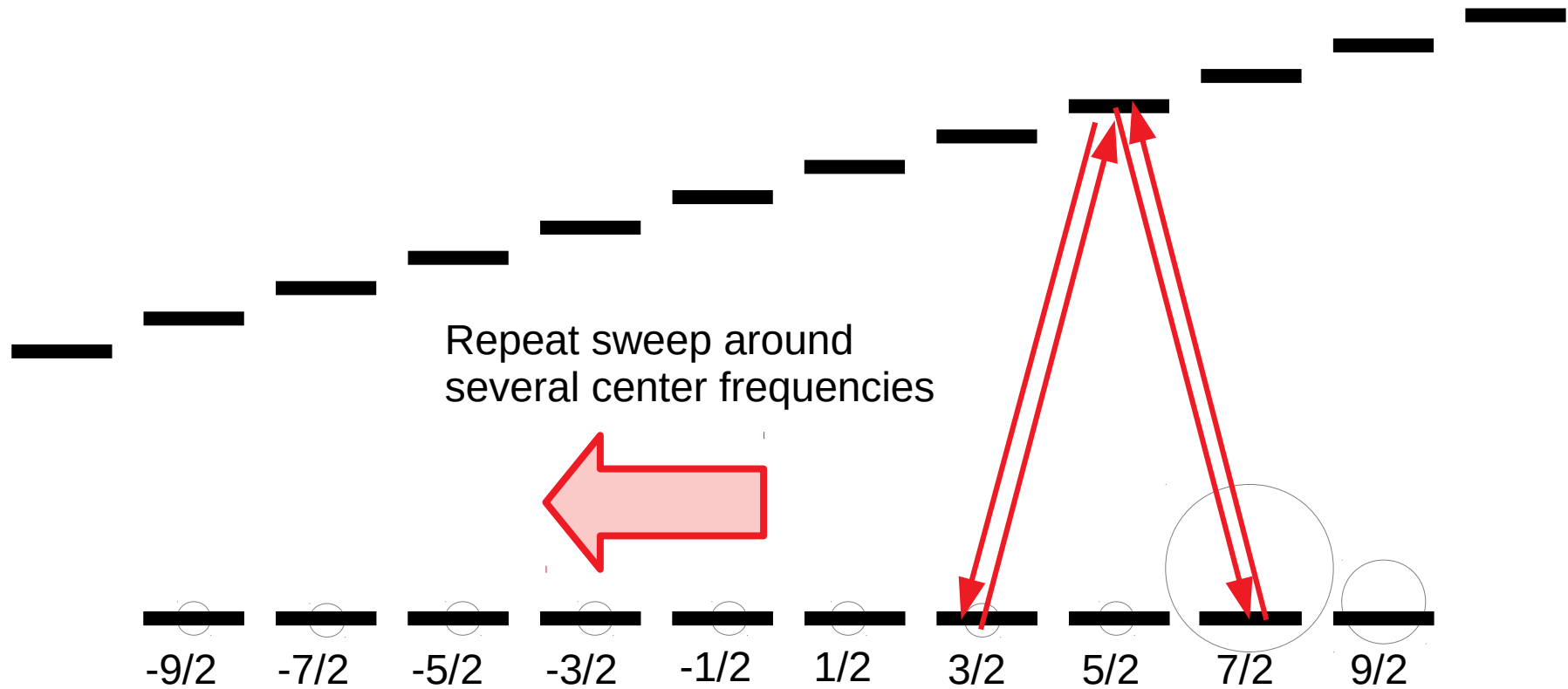
Sample from optical pumping procedure



Two spin state populations measured in one run

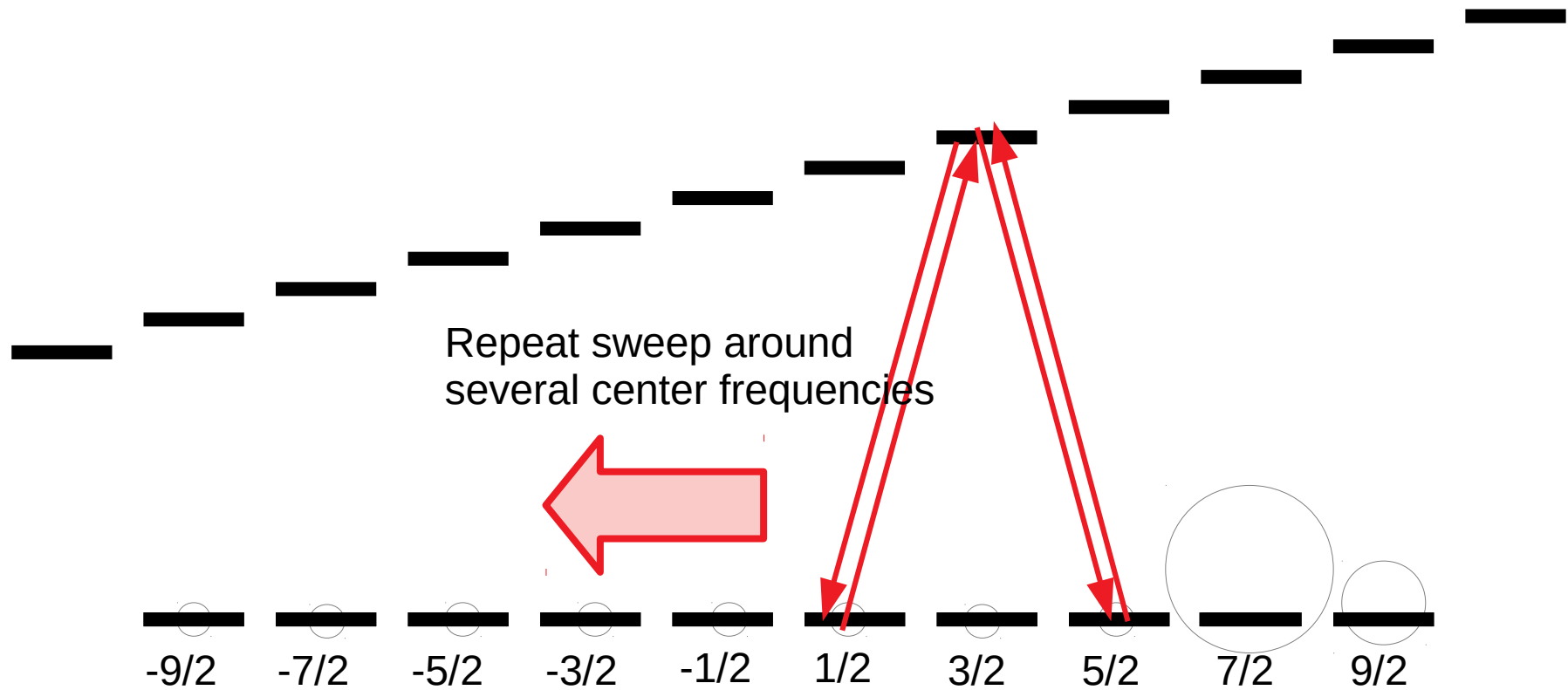
Spin state measurement

Full population measurements



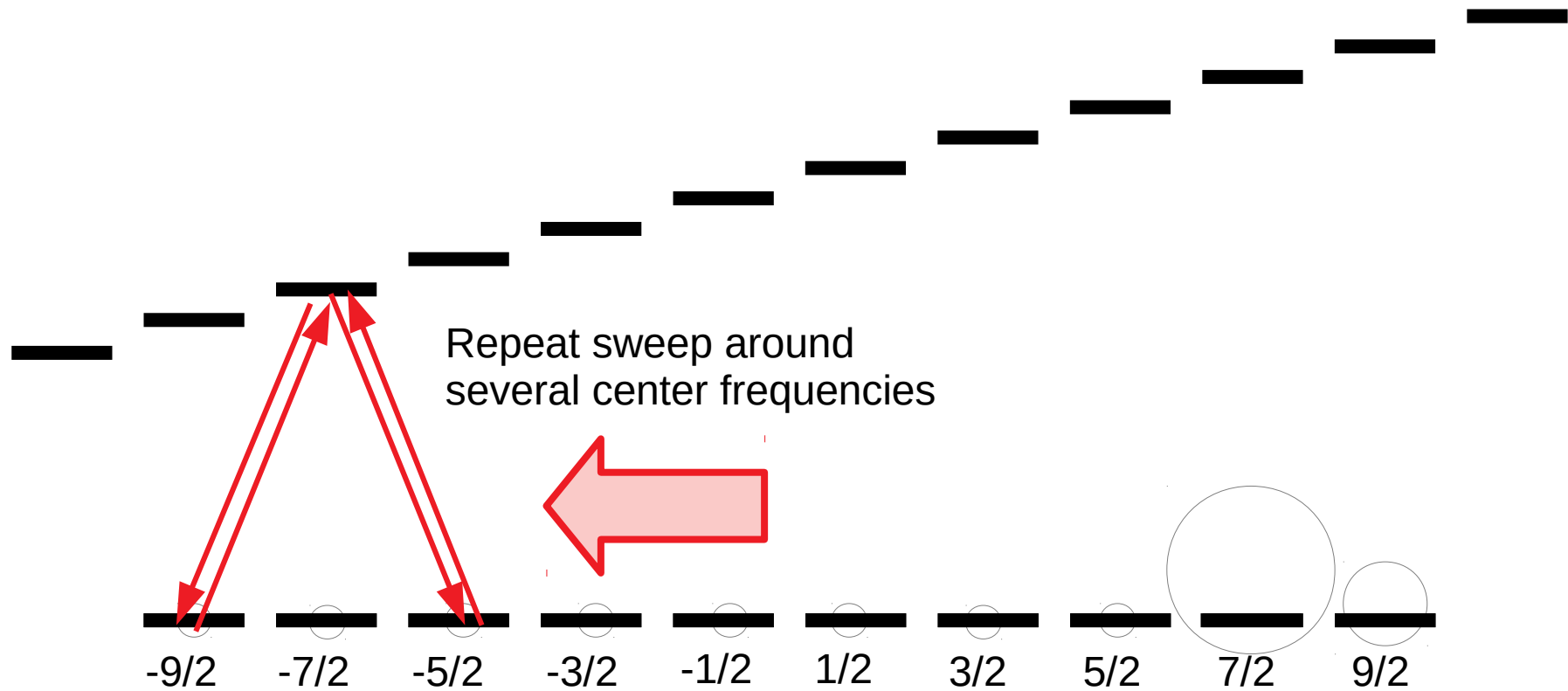
Spin state measurement

Full population measurements

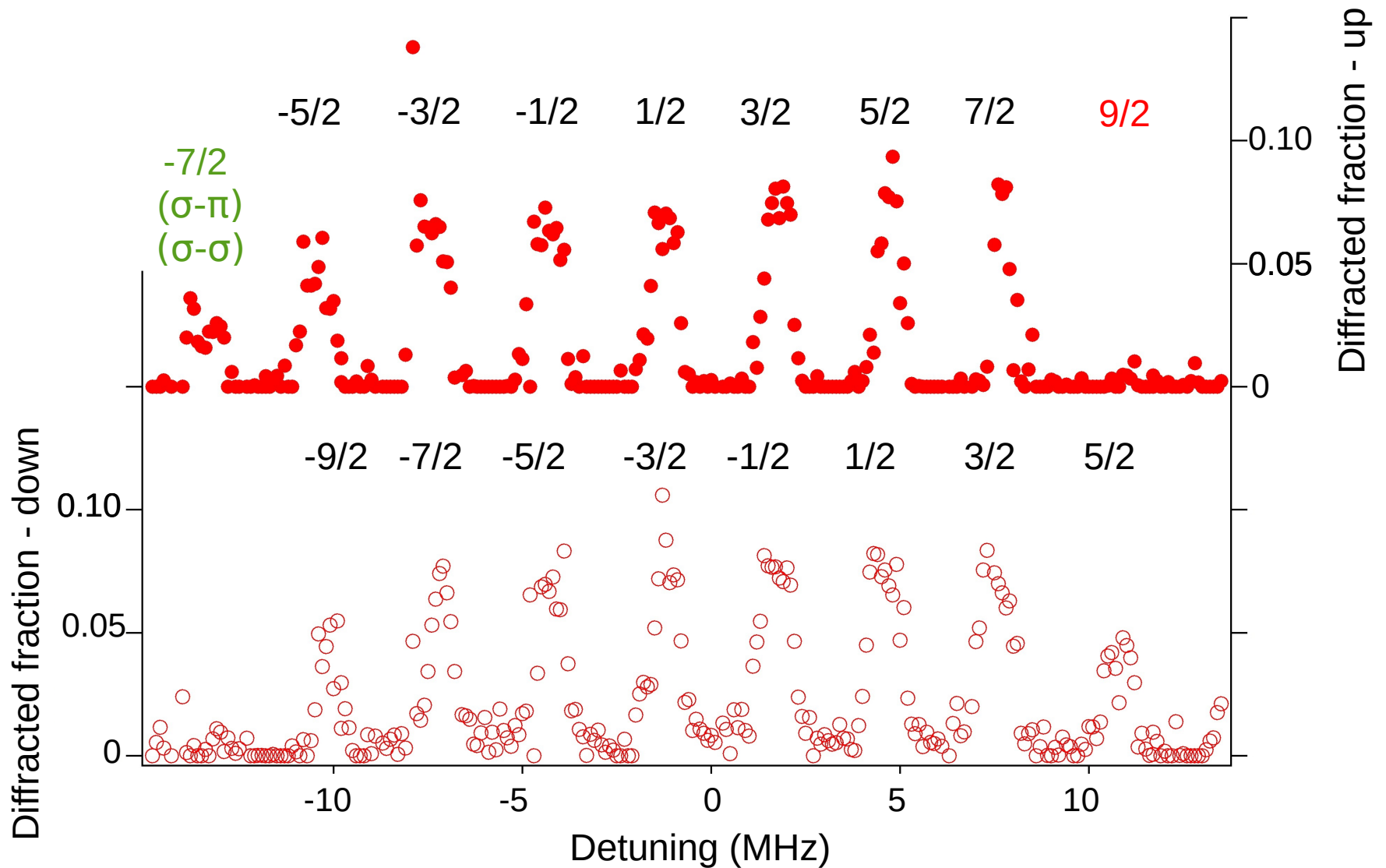


Spin state measurement

Full population measurements



Spin state measurement



Average diffraction efficiency $\sim 70\%$

Mostly limited by Laser intensity (4 mW/cm^2) / small Clebsh Gordan coefficients

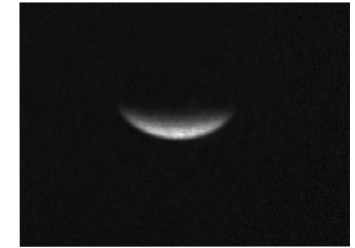
Thank you for your attention

Birth of the strontium 87 experiment at LPL

Spin 9/2 Fermi gases at $T/T_f \sim 0.2$

Adiabatic spin-dependent momentum transfer

A free-space version of our ambitions inside the optical lattice:
coherent, position-dependent manipulations of the spin degree of freedom (S.O.C)



I. Manai, P. Bataille, A. Litvinov, J. Huckans, F. Wiotte, A. Kaladjian, O. Gorceix,
E. Maréchal, M. Robert-de-Saint-Vincent, B. Laburthe-Tolra

Shelving spectroscopy of the Sr intercombination line

[ArXiv:1910.11718](https://arxiv.org/abs/1910.11718)

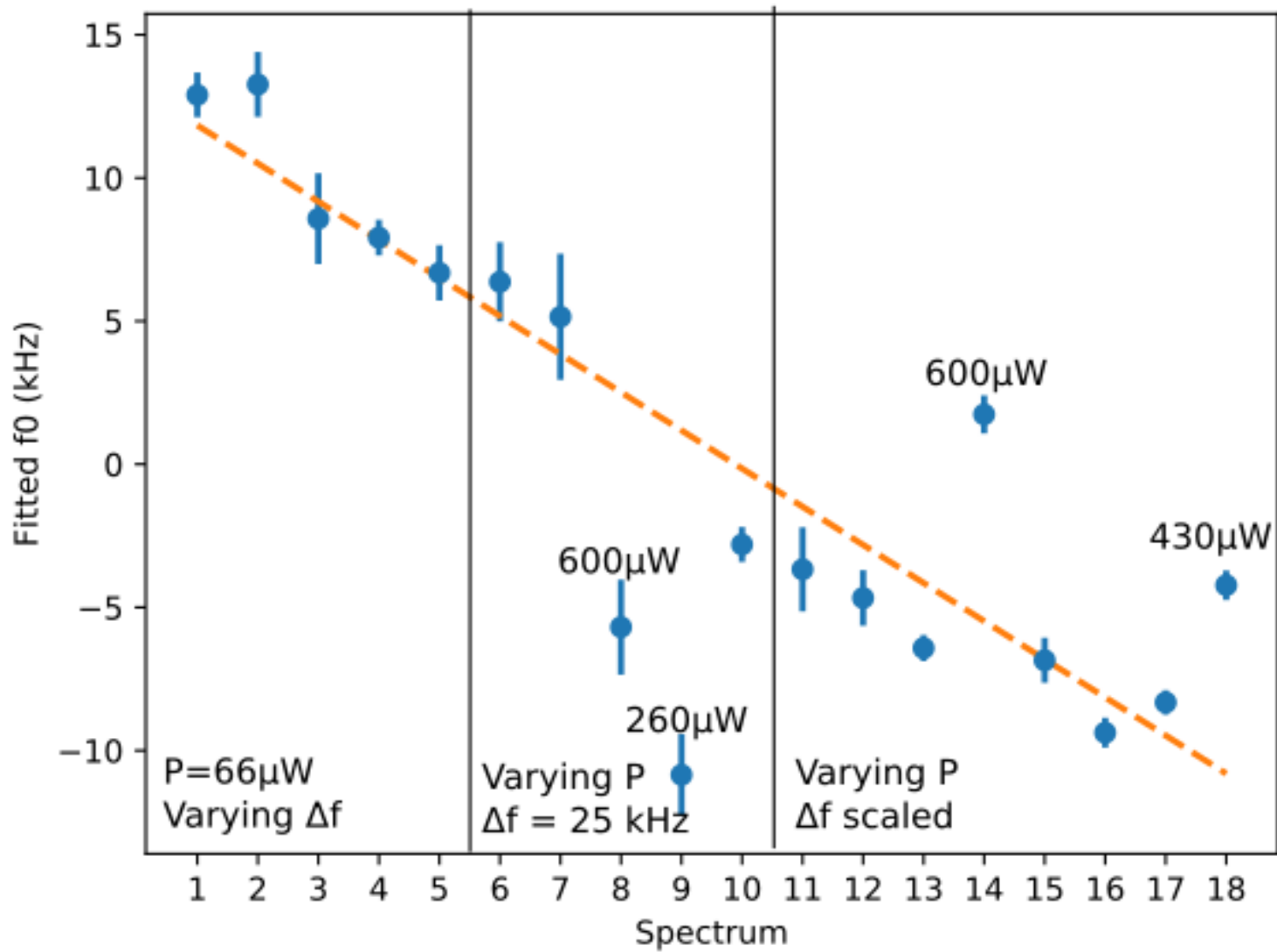
Simple scheme applicable to most Sr spectroscopy setups (cell and beam),
for a large signal enhancement

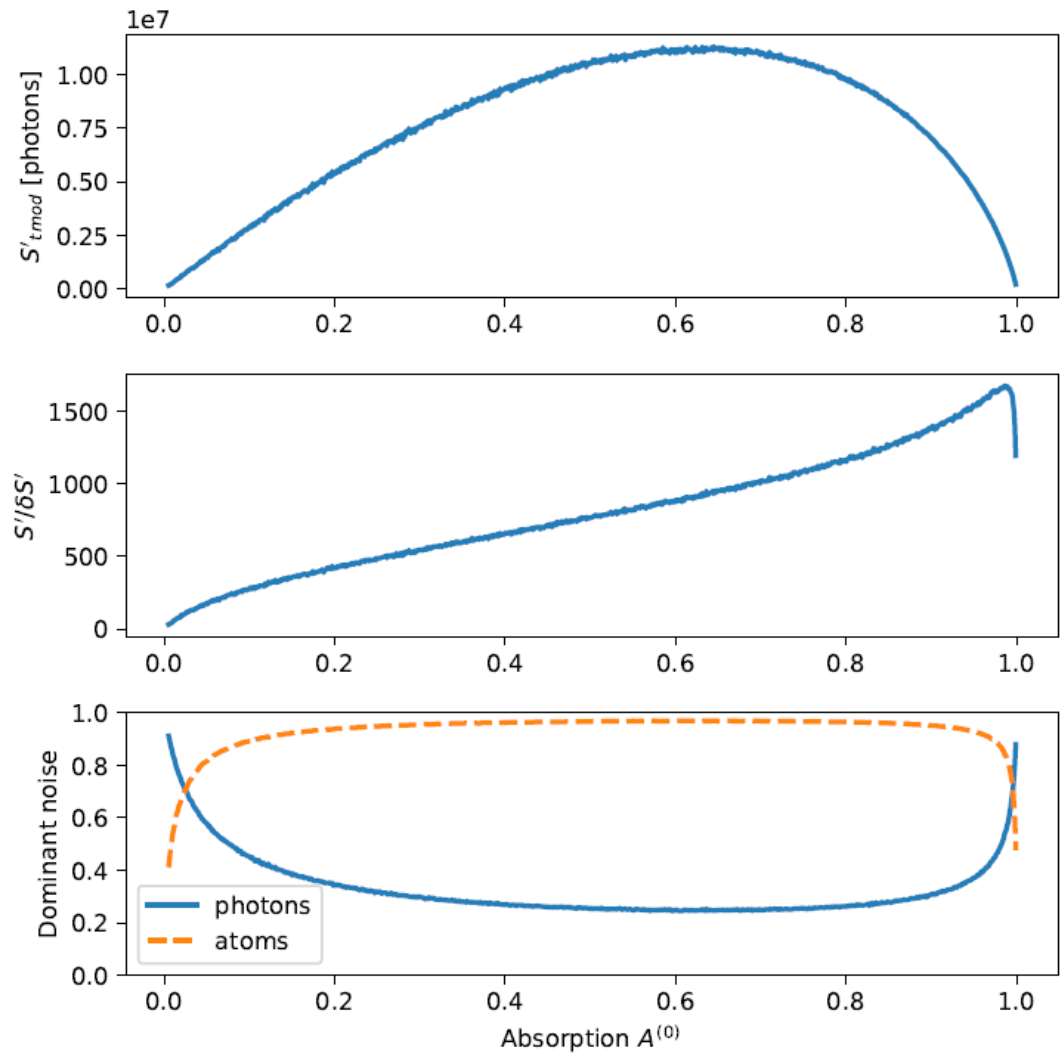
Demonstrated relative instability $2 \cdot 10^{-12}$ at 1s; expected limitations to a few 10^{-14} at 1s,
Offers perspectives for low-complexity frequency references

Manai, Duval, Bataille, Wiotte, Laburthe-Tolra, Maréchal, Robert-de-Saint-Vincent
Laboratoire de Physique des Lasers

A. Molineri, C. Briosne-Fréjaville, R. Journet, F. Nogrette, M. Cheneau
Laboratoire Charles Fabry

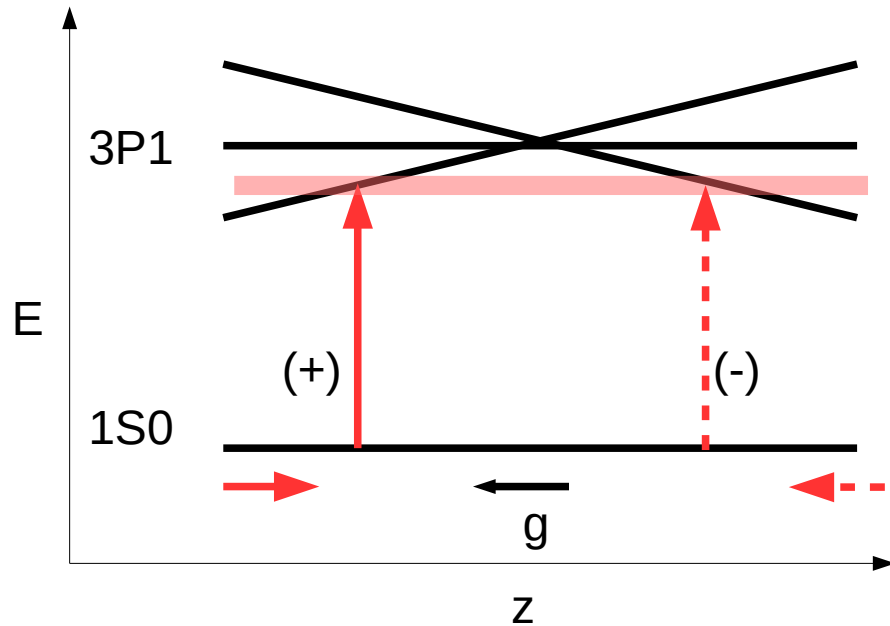
Reproducibility





Narrow-line cooling of 88 Sr

Illustrations of specificities in narrow-line MOTs



Laser cooling on a resonant shell

→ capture stage requires artificial line broadening



Tool: strong MOT compression by a frequency ramp



$F = 99$ MHz

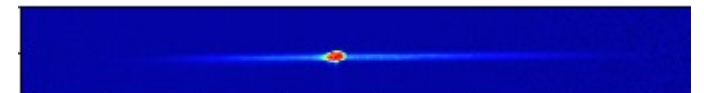


$F = 99.2$ MHz



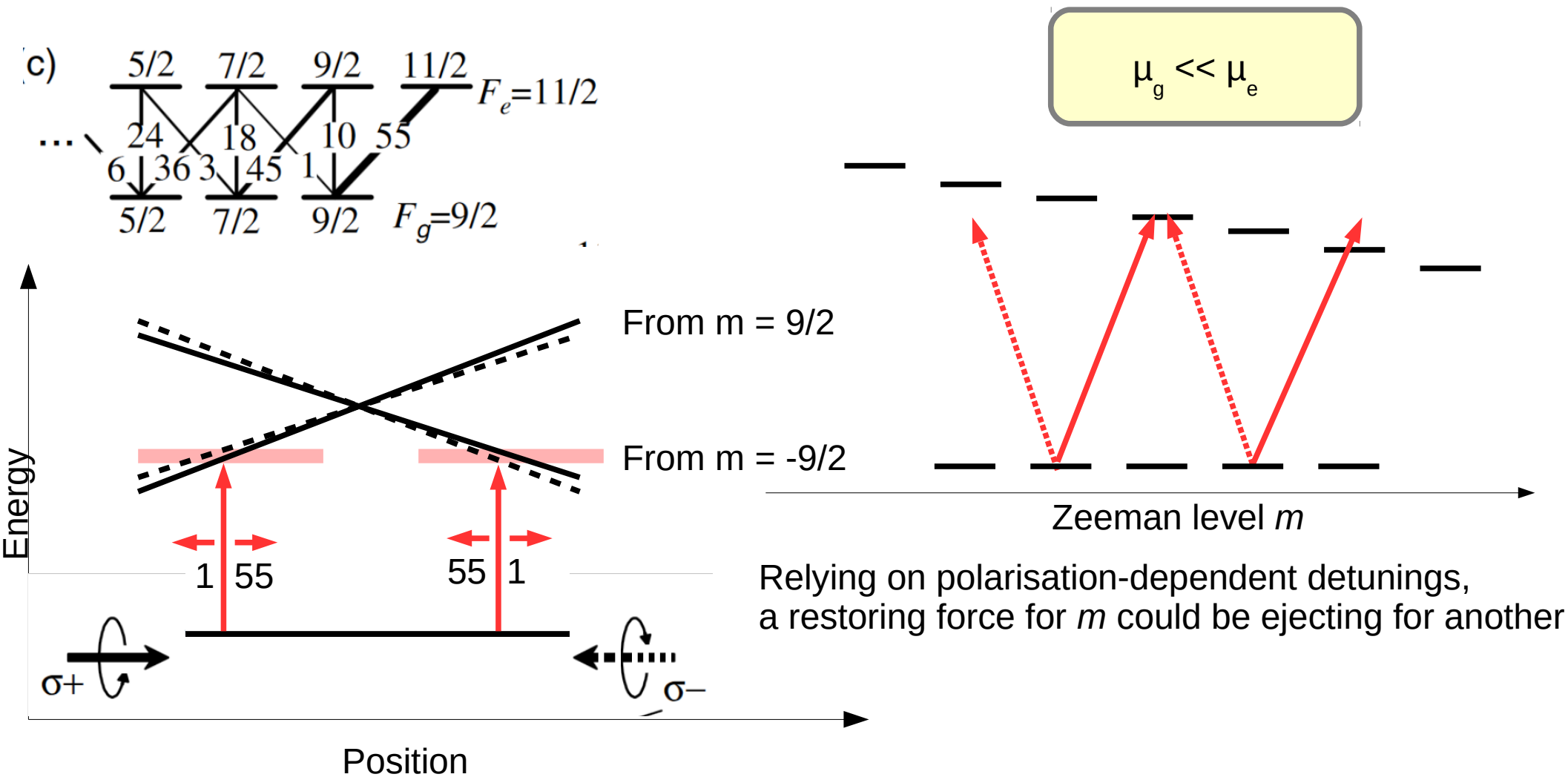
$F = 99.4$ MHz

July 2018: 88 Sr in a dipole trap



Narrow-line cooling of ^{87}Sr

Mukayami et al, PRL 90, 113002 (2003): complications from the hyperfine structure



- restoring force from Clebsh Gordan
- Only one side of the trap...

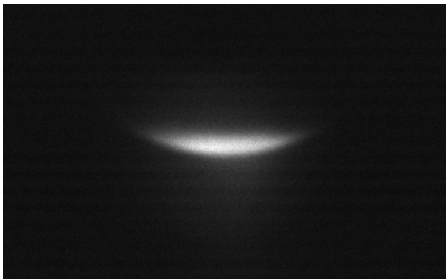


Enable spin state randomisation
Laser cooling on a second transition
with much lower Lande factor

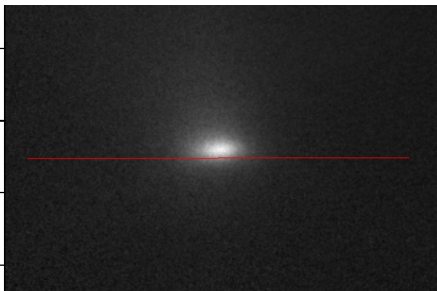
Birth of the strontium experiment

- narrow-line laser cooling ($\sim \mu\text{K}$)

^{88}Sr (May 2018)



^{87}Sr



Temperature

$$\text{Doppler limit : } k_B T \sim \frac{\hbar \Gamma}{2} \sim k_B \times 350 \text{ nK}$$

$$\text{Recoil limit: } k_B T \sim \frac{h^2}{2m\lambda^2} \sim k_B \times 460 \text{ nK}$$

Density / Phase space density

Reduced radiation trapping

$$n_0 = \frac{\kappa}{\Gamma s_0 \sigma \hbar k_L} = \frac{4}{3\pi} \frac{|\delta|}{\Gamma} \frac{\gamma_{Jb'}}{\Gamma} k_L^2.$$

Katori et al (1999) :

free space MOT, $10^{12} / \text{cm}^3$

10^{-2} phase space density

In principle ideal for loading a 3D optical trap

Ido et al (2000), Stellmer et al (2013) :

Laser cooling in dipole traps to PSD's of up to 1